Report of the Quark Flavor Physics Working Group

Conveners: J.N. Butler, Z. Ligeti, J.L. Ritchie

Task Force leaders:

V. Cirigliano, S. Kettel (Kaons); R. Briere, A. Petrov (Charm);	
A. Schwartz, T. Skwarnicki, J. Zupan (B physics);	
N. Christ, S.R. Sharpe, R.S. Van de Water (Lattice QCD)	

6	W. Altmannshofer, N. Arkani-Hamed, D.M. Asner, C. Bernard, A.J. Bevan, M. Blanke, G. Bonvicini,
7	T.E. Browder, D.A. Bryman, P. Campana, R. Cenci, D. Cline, J. Comfort, D. Cronin-Hennessy, A. Datta,
8	S. Dobbs, M. Duraisamy, A.X. El-Khadra, J.E. Fast, R. Forty, K.T. Flood, T. Gershon, B. Hamilton,
9	D.G. Hitlin, D.E. Jaffe, A. Jawahery, C.P. Jessop, A.L. Kagan, D.M. Kaplan, M. Kohl, P. Krizan,
10	A.S. Kronfeld, K. Lee, L.S. Littenberg, D.B. MacFarlane, P.B. Mackenzie, B.T. Meadows, J. Olsen,
11	M. Papucci, G. Paz, G. Perez, L.E. Piilonen, K. Pitts, M.V. Purohit, B. Quinn, B.N. Ratcliff,
12	D.A. Roberts, J.L. Rosner, P. Rubin, J. Seeman, K.K. Seth, B. Schmidt, A. Schopper, M.D. Sokoloff,
13	A. Soni, K. Stenson, S. Stone, R. Sundrum, R. Tschirhart, A. Vainshtein, Y.W. Wah, G. Wilkinson,
14	M.B. Wise, E. Worchester, J. Xu, T. Yamanaka

15

1

234

¹⁶ 1.1 Introduction

This report, from the Quark Flavor Physics working group, describes the physics case for precision studies 17 of flavor-changing interactions of bottom, charm, and strange quarks, and it discusses experimental program 18 needed to exploit these physics opportunities. It also discusses the role of theory and the importance of lattice 19 QCD to future progress in this field. The report is the result of a process that began before Snowmass, in the 20 fall of 2011 with the DOE-sponsored workshop on Fundamental Physics at the Intensity Frontier (Rockville, 21 MD). The Heavy Quarks working group from that workshop continued into the Snowmass process, albeit 22 with a change of name to Quark Flavor Physics to better reflect our emphasis on quark flavor mixing. The 23 Heavy Quarks report [1] from that workshop not only provided a starting point for our Snowmass efforts, 24 but it also provided the initial version of this report, since the physics case for quark-flavor physics and the 25 associated experimental program has not changed. 26

With the initiation of the Snowmass process, our working group grew. Also, four Task Forces were organized to focus on four closely related, but distinct, areas of effort in quark-flavor physics: kaons, charm, *B*-physics,

²⁹ and lattice QCD. Our working group had physical meetings during the Community Planning Meeting at

³⁰ Fermilab (October, 2012), at the Intensity Frontier Workshop at Argonne (April, 2013), and at Snowmass

itself at the University of Minnesota (July, 2013). Consequently, this report is the culmination of discussions

³² that were conducted over a period of almost two years.

This report describes the physics case for quark-flavor physics, and it represents the aspirations of a substantial community of physicists in the U.S. who are interested in this physics. This report is not a review of quark-flavor physics, and no attempt has been made to provide complete references to prior work. Rather, it focuses on the opportunities for spectacular discoveries during the remainder of this decade and during the next decade, made possible by the extraordinary reach to high mass scales that is possible in guark flavor physics cupating the remainder of the spectacular discoveries during the remainder of the scale scal

³⁸ quark-flavor physics experiments.

Nevertheless, before looking forward, it provides useful context to briefly review some history. In the 1990's, 39 the U.S. was the leader both on the Energy Frontier and in quark flavor-physics experiments at the Intensity 40 Frontier. B physics was still dominated by the CLEO experiment for most of that decade. The most 41 sensitive rare K decay experiments performed to date were then underway at the Brookhaven AGS, and 42 direct CP violation in $K_L^0 \to \pi\pi$ decays was the focus of a fixed-target experiment using the Tevatron at 43 Fermilab. Toward the end of that decade, the asymmetric e^+e^- B factories began running at SLAC and 44 KEK, leading to increases in the size of B meson datasets by two orders of magnitude and also opening the 45 door to measurements of time-dependent CP asymmetries, which provided the experimental basis for the 46 2008 Nobel Prize. In the midst of this success, a number of new and aggressive quark-flavor initiatives were 47 put forward in the U.S. These included the BTeV proposal which would have used the Tevatron collider for 48 B physics, the CKM proposal which would have made the first high-statistics measurement of $K^+ \to \pi^+ \nu \overline{\nu}$ 49 using the Fermilab Main Injector, and the RSVP proposal which included an experiment (KOPIO) to 50 measure $K_L^0 \to \pi^0 \nu \overline{\nu}$ at the Brookhaven AGS. After lengthy consideration in an environment characterized 51 by flat budgets and a predilection for a fast start on the International Linear Collider on U.S. soil, all of these 52 initiatives were ultimately terminated. Also, as accelerator breakthroughs capable of increasing B-factory 53 luminosity by more than another order of magnitude were made, the opportunity to upgrade the PEP-II 54 B factory at SLAC was not pursued. This history is relevant in order to stress that the U.S. has been a 55 leader in flavor-physics experiments — involving a vigorous community — until very recently. Nonetheless, 56 this sequence of events inevitably encouraged many in the flavor-physics community in the U.S. to migrate 57 elsewhere, most often to ATLAS or CMS at the LHC. 58

⁵⁹ In spite of these developments in the U.S., a rich heavy-quark flavor physics program is flourishing around ⁶⁰ the world. Kaon experiments, *B*-physics experiments, and charm experiments are running and under ⁶¹ construction in Asia and Europe. Indeed, CERN — the laboratory that now owns the Energy Frontier — ⁶² is also the home of a running *B*-physics experiment (LHCb), which has a clear upgrade path, and a rare *K* ⁶³ decay experiment (NA62) which will begin taking data in parallel with LHC running in 2014. This reflects ⁶⁴ the world-wide consensus that flavor-physics experiments are critical to progress in particle physics.

Looking forward, it is clear that there continues to be strong interest and a potentially substantial community 65 in the U.S. for an Intensity Frontier flavor-physics program. The basic motivation for this program can be 66 described very simply. If the LHC observes new high-mass states, it will be necessary to distinguish between 67 models proposed to explain them. This will require tighter constraints from the flavor sector, which can 68 come from more precise experiments using strange, charm, and bottom quark systems. If the LHC does not 69 make such discoveries, then the ability of precision flavor-physics experiments to probe mass scales far above 70 LHC, through virtual effects, is the best hope to see signals that may point toward the next energy scale to 71 explore. 72

In the following sections of this report, we describe the general physics case for quark-flavor physics, followed
 by the reports of each of the Task Forces. The Task Forces were in communication with each other, but

vorked independently on these reports. Finally, this report concludes with a discussion of how the U.S.

⁷⁶ high-energy physics program can, at relatively modest cost compared to most other initiatives, participate

 π in critical flavor-physics experiments offshore and regain a some of its leadership status by executing a

⁷⁸ program of rare kaon decay experiments at Fermilab.

⁷⁹ 1.2 Quark Flavor as a Tool for Discovery

An essential feature of flavor physics experiments is their ability to probe very high mass scales, beyond 80 the energy accessible in collider experiments. In addition, flavor physics can teach us about properties of 81 TeV-scale new physics, which cannot be learned from the direct production of new particles at the LHC. 82 This is because quantum effects allow virtual particles to modify the results of precision measurements in 83 ways that reveal the underlying physics. (The determination of the t-s, d couplings in the standard model 84 (SM) exemplifies how direct measurements of some properties of heavy particles may only be possible in 85 flavor physics.) Even as the LHC embarks on probing the TeV scale, the ongoing and planned precision 86 flavor physics experiments are sensitive to beyond standard model (BSM) interactions at mass scales which 87 are higher by several orders of magnitude. These experiments will provide essential constraints and comple-88 mentary information on the structure of models put forth to explain any discoveries at LHC, and they have 89 the potential to reveal new physics that is inaccessible to the LHC. 90

Throughout the history of particle physics discoveries made in studies of rare processes have led to new and 91 deeper understanding of nature. A classic example is beta decay, which foretold the electroweak mass scale 92 and the ultimate observation of the W boson. Results from kaon decay experiments were crucial for the 93 development of the standard model: the discovery of CP violation in $K_L^0 \to \pi^+\pi^-$ decay ultimately pointed 94 toward the three-generation CKM model [2, 3], the absence of strangeness-changing neutral current decays 95 (i.e., the suppression of $K_L^0 \to \mu^+ \mu^-$ with respect to $K^+ \to \mu^+ \nu$) led to the prediction of a fourth quark [4] 96 (charm), and the measured value of the $K_L - K_S$ mass difference made it possible to predict the charm 97 quark mass [5, 6] before charm particles were directly detected. More recently the larger than expected 98 $B_H - B_L$ mass difference foretold the high mass of the top quark. Precision measurements of time-dependent 99 CP-violating asymmetries in B-meson decays in the BABAR and Belle experiments firmly established the 100 CKM phase as the dominant source of CP violation observed to date in flavor-changing processes — leading 101 to the 2008 Nobel Prize for Kobayashi and Maskawa. At the same time, corrections to the SM at the tens of 102 percent level are still allowed, and many extensions of the SM proposed to solve the hierarchy problem are 103 likely to give rise to changes in flavor physics that may be observed in the next generation of experiments. 104

¹⁰⁵ 1.2.1 Strange, Charm, and Bottom Quarks as Probes for New Physics

In the past decade our understanding of flavor physics has improved significantly due to the e^+e^- B factories, 106 BABAR, Belle, CLEO, the Tevatron experiments, and most recently LHCb. While kaon physics was crucial 107 for the development of the SM, and has provided some of the most stringent constraints on BSM physics 108 since the 1960s, precision tests of the CKM picture of CP violation in the kaon sector have been hindered 109 by theoretical uncertainties in calculating direct CP violation (ϵ'). The B factories provided many stringent 110 tests by precisely measuring numerous CP-violating and CP-conserving quantities, which in the SM are 111 determined in terms of just a few parameters, but are sensitive to different possible BSM contributions. The 112 consistency of the measurements and their agreement with CP violation in $K^0 - \overline{K}^0$ mixing, ϵ_K , and with the 113 SM predictions (shown in the left plot in Fig. 1-1) strengthened the "new physics flavor problem". It is the 114 tension between the relatively low (TeV) scale required to stabilize the electroweak scale, and the high scale 115 that is seemingly required to suppress BSM contributions to flavor-changing processes. This problem arises 116 because the SM flavor structure is very special, containing small mixing angles, and because of additional 117 strong suppressions of flavor-changing neutral-current (FCNC) processes. Any TeV-scale new physics must 118 preserve these features, which are crucial to explain the observed pattern of weak decays. 119

	Bounds on Λ [TeV] ($C = 1$)		Bounds on C ($\Lambda = 1 \mathrm{TeV}$)			
Operator	Re	Im	Re	Im	Observables	
$\overline{(\bar{s}_L \gamma^\mu d_L)^2}$	9.8×10^2	$1.6 imes 10^4$	$9.0 imes 10^{-7}$	3.4×10^{-9}	$\Delta m_K; \epsilon_K$	
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	$1.8 imes 10^4$	$3.2 imes 10^5$	$6.9 imes 10^{-9}$	2.6×10^{-11}	$\Delta m_K; \epsilon_K$	
$\overline{(\bar{c}_L \gamma^\mu u_L)^2}$	1.2×10^3	2.9×10^3	$5.6 imes 10^{-7}$	$1.0 imes 10^{-7}$	$\Delta m_D; q/p , \phi_D$	
$(\bar{c}_R u_L)(\bar{c}_L u_R)$	6.2×10^3	$1.5 imes 10^4$	$5.7 imes 10^{-8}$	1.1×10^{-8}	$\Delta m_D; q/p , \phi_D$	
$(\bar{b}_L \gamma^\mu d_L)^2$	5.1×10^2	$9.3 imes 10^2$	3.3×10^{-6}	1.0×10^{-6}	$\Delta m_{B_d}; S_{\psi K_S}$	
$(\bar{b}_R d_L) (\bar{b}_L d_R)$	$1.9 imes 10^3$	$3.6 imes10^3$	$5.6 imes10^{-7}$	$1.7 imes 10^{-7}$	$\Delta m_{B_d}; S_{\psi K_S}$	
$(\bar{b}_L \gamma^\mu s_L)^2$	$1.1 imes 10^2$	$??2.2\times10^2$	$7.6 imes10^{-5}$	$??1.7 imes10^{-5}$	$\Delta m_{B_s}; S_{\psi\phi}$	
$(ar{b}_R s_L)(ar{b}_L s_R)$	$3.7 imes 10^2$	$??7.4\times10^2$	$1.3 imes 10^{-5}$	$??3.0\times10^{-6}$	$\Delta m_{B_s}; S_{\psi\phi}$	

Table 1-1. Bounds on $\Delta F = 2$ operators of the form $(C/\Lambda^2) \mathcal{O}$, with \mathcal{O} given in the first column. The bounds on Λ assume C = 1, the bounds on C assume $\Lambda = 1$ TeV. (From Ref. [7], with some LHCb updates.)

The motivation for a broad program of precision flavor physics measurements has gotten even stronger in 120 light of the first LHC run. With the discovery of a new particle whose properties are similar to the SM Higgs 121 boson, but no sign of other high-mass states, the LHC has begun to test naturalness as a guiding principle 122 of BSM research. If the electroweak scale is unnatural, we have little information on the next energy scale 123 to explore (except for a hint at the TeV scale from dark matter, a few anomalous experimental results, and 124 neutrinos most likely pointing at a very high scale). The flavor physics program will explore much higher 125 scales than can be directly probed. However, if the electroweak symmetry breaking scale is stabilized by a 126 natural mechanism, new particles should be found at the LHC. Since the largest quantum correction to the 127 Higgs mass in the SM is due to the top quark, the new particles will likely share some properties of the SM 128 quarks, such as symmetries and interactions. Then they would provide a novel probe of the flavor sector, 129 and flavor physics and the LHC data would provide complementary information. Their combined study is 130 our best chance to learn more about the origin of both electroweak and flavor symmetry breaking. 131

Consider, for example, a model in which the only suppression of new flavor-changing interactions comes 132 from the large masses of the new particles that mediate them (at a scale $\Lambda \gg m_W$). Flavor physics, 133 in particular measurements of meson mixing and CP violation, put severe lower bounds on Λ . For some 134 of the most important four-quark operators contributing to the mixing of the neutral K, D, B, and B_s 135 mesons, the bounds on the coefficients C/Λ^2 are summarized in Table 1-1. For C = 1, they are at the 136 scale $\Lambda \sim (10^2 - 10^5)$ TeV. Conversely, for $\Lambda = 1$ TeV, the coefficients have to be very small. Therefore, 137 there is a tension. The hierarchy problem can be solved with new physics at $\Lambda \sim 1 \text{ TeV}$. Flavor bounds, 138 however, require much larger scales, or tiny couplings. This tension implies that TeV-scale new physics 139 must have special flavor structures, e.g., possibly sharing some of the symmetries that shape the SM Yukawa 140 interactions. The new physics flavor puzzle is thus the question of why, and in what way, the flavor structure 141 of the new physics is non-generic. As a specific example, in a supersymmetric extension of the SM, there are 142 box diagrams with winos and squarks in the loops. The size of such contributions depends crucially on the 143 mechanism of SUSY breaking, which we would like to probe. 144

To be sensitive to BSM contributions to FCNC processes (where the SM is suppressed, but not absent), many measurements need to be done, and it is only their combination that can reveal a signal. (There are some exceptions, mainly processes forbidden in the SM, but considering only those would reduce the sensitivity of the program to BSM physics.) To visualize the constraints from many measurements, it is convenient to

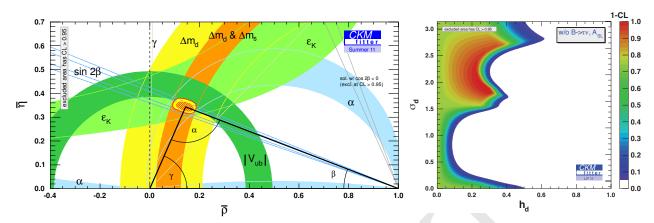


Figure 1-1. [will be updated] Left: Constraints on the apex of the unitarity triangle in the $\bar{\rho} - \bar{\eta}$ plane (at 95% CL). Right: the allowed $h_d - \sigma_d$ new physics parameter space (see text) in $B^0 - \bar{B}^0$ mixing. (From Refs. [8, 9].)

¹⁴⁹ use the Wolfenstein parameterization [10] of the CKM matrix (for a review, see [11]),

$$V_{\rm CKM} = \begin{pmatrix} V_{ud} \ V_{us} \ V_{ub} \\ V_{cd} \ V_{cs} \ V_{cb} \\ V_{td} \ V_{ts} \ V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\bar{\rho} - i\bar{\eta}) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \bar{\rho} - i\bar{\eta}) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4) \,. \tag{1.1}$$

It exhibits the hierarchical structure of the CKM matrix by expanding in a small parameter, $\lambda \simeq 0.23$. The unitarity of this matrix in the SM implies many relations, such as that defining the "unitarity triangle" shown in Fig. 1-1, which arises from rescaling $V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$ by $V_{cd} V_{cb}^*$ and choosing two vertices of the resulting triangle to be (0,0) and (1,0).

As a result of second-order weak interaction processes, there are transitions between the neutral meson flavor 154 eigenstates, so the physical mass eigenstates are their linear combinations, denoted as $|B_{H,L}\rangle = p|B^0\rangle \mp q|\overline{B^0}\rangle$. 155 (The p and q parameters differ for the four neutral mesons, but the same notation is commonly used without 156 distinguishing indices.) In a large class of models, the BSM physics modifies the mixing amplitude of neutral 157 mesons, and leaves tree-level decays unaffected. This effect can be parameterized by just two real parameters for each mixing amplitude. For $B^0 - \overline{B}^0$ mixing, writing $M_{12} = M_{12}^{\text{SM}} \left(1 + h_d e^{2i\sigma_d}\right)$, the constraints on h_d and σ_d are shown in the right plot in Fig. 1-1. (Evidence for $h_d \neq 0$ would rule out the SM.) Only in 158 159 160 2004, after the first significant constraints on γ and α from BABAR and Belle, did we learn that the BSM 161 contribution to $B-\overline{B}$ mixing must be less than the SM amplitude [12, 9]. The right plot in Fig. 1-1 shows 162 that order 20% corrections to $|M_{12}|$ are still allowed for (almost) any value of the phase of the new physics 163 contribution, and if this phase is aligned with the SM ($\sigma_d = 0 \mod \pi/2$), then the new physics contribution 164 does not yet have to be much smaller than the SM one. Similar conclusions apply to other neutral meson 165 mixings [13, 14], as well as many other $\Delta F = 1$ FCNC transition amplitudes. 166

¹⁶⁷ The fact that such large deviations from the SM are not yet excluded gives very strong motivations to ¹⁶⁸ continue flavor physics measurements in order to observe deviations from the SM predictions or establish an ¹⁶⁹ even stronger hierarchy between the SM and new physics contributions.

¹⁷⁰ In considering the future program, the following issues [15] are of key importance:

171 1. What are the expected deviations from the SM predictions induced by new physics at the TeV scale? As explained above, TeV-scale new physics with generic flavor structure is ruled out by many orders of magnitudes. However, sizeable deviations from the SM are still allowed by the current bounds, and in many scenarios observable effects are expected.

- 175 2. What are the theoretical uncertainties?
- These are highly process dependent. Some measurements are limited by theoretical uncertainties (due to hadronic, strong interaction, effects), but in many key processes the theory uncertainties are very small, below the expected sensitivity of future experiments.
- 3. What can be expected in terms of experimental precision?
- The useful data sets can increase by a factor of order 100 (in most cases 10–1000), and will probe effects predicted by fairly generic BSM scenarios.
- ¹⁸² 4. What will the measurements reveal, if deviations from the SM are [not] seen?
- The flavor physics data will be complementary with the high- p_T part of the LHC program. The synergy of measurements can reveal a lot about what the new physics at the TeV scale is, and what it is not.

This report concentrates on the physics and prospects of a subset of measurements, for which the answers to these questions are the clearest, both in terms of theoretical cleanliness and experimental feasibility. The experiments will enable many additional measurements which are not discussed here, some due to lack of space, and some because they will be more important than can now be anticipated. (Recall that the best measurements of the CKM angles α and γ at *BABAR* and Belle were not in formerly expected decay modes.) While future theory progress is important, the value of more sensitive experiments is not contingent on it.

¹⁹¹ 1.2.2 The Role of Theory

To find a convincing deviation from the SM, a new physics effect has to be several times larger than the 192 experimental uncertainty of the measurement and the theoretical uncertainty of the SM prediction. One 193 often distinguishes two kinds of theoretical uncertainties, perturbative and nonperturbative (this separation 194 is not unambiguous). Perturbative uncertainties come from the truncation of expansions in small (or not-195 so-small) coupling constants, such as α_s at a few GeV scale. There are always higher order terms that 196 have not been computed. Nonperturbative effects arise because QCD becomes strongly interacting at low 197 energies. These are often the limiting uncertainties, since, in general, there is no systematic method to 198 calculate them model independently. There are, nevertheless, several possibilities to get at the fundamental 199 physics in certain cases, even in the presence of such uncalculable effects. 200

- For some observables the hadronic parameters (mostly) cancel, or can be extracted from data (e.g., using the measured $K \to \pi \ell \nu$ form factor to predict $K \to \pi \nu \bar{\nu}$, several methods to extract γ , etc.).
- In many cases, CP invariance of the strong interaction implies that the dominant hadronic physics cancels, or is CKM suppressed (e.g., measuring β from $B \to \psi K_S$, and some other CP asymmetries).
- In some cases one can use symmetries of the strong interaction which arise in certain limits, such as the chiral limit or the heavy quark limit, to establish that nonperturbative effects are suppressed by small parameters and to estimate them (e.g., measuring $|V_{us}|$ and $|V_{cb}|$, inclusive *B* decays).

• Lattice QCD is a model independent method to address nonperturbative phenomena. In practice, the most robust results are for matrix elements involving at most one hadron in the initial and the final state (allowing, e.g., extractions of magnitudes of CKM elements).

All of these approaches use experimental data from related processes to fix some parameters, constrain the uncertainties, and cross-check the methods. Thus, experimental progress on a broad program will not only reduce the uncertainties of key measurements, but also help reduce theoretical uncertainties.

As an example, consider extracting γ from $B \to DK$. This is one of the cleanest measurement in terms of theoretical uncertainties, because all the necessary hadronic quantities can be measured. All $B \to DK$ ²¹⁶ based analyses considers decays of the type $B \to D(\overline{D}) K(X) \to f_D K(X)$, where f_D is a final state that ²¹⁷ is accessible in both D and \overline{D} decay, allowing for interference, and X represents possible extra particles in ²¹⁸ the final state. Using several $B \to DKX$ decays modes (say, n different X states and k different D and \overline{D} ²¹⁹ decay modes), one can perform nk measurements, which depend on n + k decay amplitudes. Thus, one can ²²⁰ determine all hadronic parameters, as well as the weak phase γ , with very little theoretical uncertainty.

The main reason why many CP asymmetry measurements have small theoretical uncertainties is because 221 they involve ratios of rates, from which the leading amplitudes cancel, so the uncertainties are suppressed by 222 the relative magnitude of the subleading amplitudes. This is the case for the time dependent CP asymmetry 223 in $B \to \psi K_S$, in which case the subdominant amplitude is suppressed by a factor ~ 50 due to CKM elements 224 and by the ratio of the matrix element of a loop diagram compared to a tree diagram. However, it is not 225 simple to precisely quantify the uncertainties below the percent level. In other modes (e.g., $B \to \phi K_S$, $\eta' K_S$, 226 etc.) the loop suppression of the hadronic uncertainty is absent, and the theoretical understanding directly 227 impacts at what level new physics can be unambiguously observed. 228

229 Symmetries of the strong interaction that occur for hadrons containing light quarks $(m_{u,d,s} < \Lambda_{\text{QCD}})$ or for

hadrons containing a heavy quark $(m_{b,c} > \Lambda_{QCD})$ have played critical roles in understanding flavor physics. 230 Chiral perturbation theory has been very important for kaon physics, and isospin symmetry is crucial for 231 the determination of α in $B \to \pi\pi$, $\rho\rho$, and $\rho\pi$ decays. For B and D mesons, extra symmetries of the 232 Lagrangian emerge in the $m_{b,c} \gg \Lambda_{\rm QCD}$ limit, and these heavy quark spin-flavor symmetries imply, for 233 example, that exclusive semileptonic $B \to D^{(*)} \ell \bar{\nu}$ decays are described by a single universal Isgur-Wise 234 function in the symmetry limit. For inclusive semileptonic B decays, an operator product expansion can be 235 used to compute sufficiently inclusive rates; applications include the extraction of $|V_{cb}|$. As is often the case. 236 after understanding the symmetry limit and its implications, it is the analysis of subleading effects where 237 many of the theoretical challenges lie. 238

Lattice QCD has become an important tool for flavor physics, and significant improvements are expected in 239 the coming years. As investment in substantial computational infrastructure is required, a separate section 240 discusses it in this report. Lattice QCD allows in principle model independent calculations of nonperturbative 241 phenomena. In practice, approximations have to be used to keep the computational time under control, e.g., 242 because the b quark is too heavy to be simulated directly. Due to new algorithms and more powerful 243 computers, matrix elements which contain at most one (stable) hadron in the final state should soon be 244 calculable with percent level uncertainties. Matrix elements involving states with sizable widths, e.g., ρ and 245 K^* , are more challenging. So are calculations of matrix elements containing more than one hadron in the 246 final state, and it will require major developments to obtain small uncertainties for those. Thus, lattice QCD 247 errors are expected to become especially small for leptonic and semileptonic decays, and meson mixing. 248

In summary, there are many observables with theoretical uncertainties at the few percent level, matching the
 expected experimental sensitivity, which is necessary to allow a discovery of small new physics contributions.
 The full exploitation of the experimental program requires continued support of theoretical developments.

²⁵² 1.3 Report of the Kaon Task Force

Kaon decays have played a pivotal role in shaping the Standard Model (SM). Prominent examples include the introduction of internal "flavor" quantum numbers (strangeness), parity violation ($K \rightarrow 2\pi, 3\pi$ puzzle), quark mixing, meson-antimeson oscillations, discovery of CP violation, suppression of flavor-changing neutral currents (FCNC), discovery of the GIM (Glashow-Iliopoulos-Maiani) mechanism and prediction of charm. Now and looking ahead, kaons continue to have high impact in constraining the flavor sector of possible extensions of the SM.

Observable	SM Theory	Current Expt.	Future Experiments
$\mathcal{B}(K^+ \to \pi^+ \nu \overline{\nu})$	$7.81(75)(29) \times 10^{-11}$	$1.73^{+1.15}_{-1.05} \times 10^{-10}$	${\sim}10\%$ at NA62
		E787/E949	${\sim}5\%$ at ORKA
			${\sim}2\%$ at Project-X
$\mathcal{B}(K^0_L \to \pi^0 \nu \overline{\nu})$	$2.43(39)(6) \times 10^{-11}$	$< 2.6 \times 10^{-8}$ E391a	1 st observation at KOTO
			${\sim}5\%$ at Project-X
$\mathcal{B}(K_L^0 \to \pi^0 e^+ e^-)$	$(3.23^{+0.91}_{-0.79}) \times 10^{-11}$	$< 2.8 \times 10^{-10}$ KTeV	${\sim}10\%$ at Project-X
${\cal B}(K^0_L\to\pi^0\mu^+\mu^-)$	$(1.29^{+0.24}_{-0.23}) \times 10^{-11}$	$< 3.8 \times 10^{-10}$ KTeV	${\sim}10\%$ at Project-X
$ P_T $	$\sim 10^{-7}$	< 0.0050	< 0.0003 at TREK
in $K^+ \to \pi^0 \mu^+ \nu$			< 0.0001 at Project-X
$\Gamma(K_{e2})/\Gamma(K_{\mu 2})$	$2.477(1) \times 10^{-5}$	$2.488(12) \times 10^{-5}$	$\pm 0.0054 \times 10^{-5}$ at TREK
		(NA62, KLOE)	$\pm 0.0025 \times 10^{-5}$ at Project-X
$\mathcal{B}(K_L^0 \to \mu^{\pm} e^{\mp})$	$< 10^{-25}$	$< 4.7 \times 10^{-12}$	$< 2 \times 10^{-13}$ at Project-X

Table 1-2. A summary of the reach of current and proposed experiments for some key rare kaon decay measurements, in comparison to standard model theory and the current best experimental results. In the SM predictions for the $K \to \pi \nu \bar{\nu}$ and $K \to \pi \ell^+ \ell^-$ the first error is parametric, the second denotes the intrinsic theoretical uncertainty.

In the arena of kaon decays, a key role is played by the FCNC modes mediated by the quark-level processes $s \to d(\gamma, \ell^+ \ell^-, \nu \bar{\nu})$, and in particular the four theoretically cleanest modes $K^+ \to \pi^+ \nu \bar{\nu} \ K_L \to \pi^0 \nu \bar{\nu}$, $K_L \to \pi^0 e^+ e^-, \ K_L \to \pi^0 \mu^+ \mu^-$. Because of the peculiar suppression of the SM amplitude (top-quark loop suppressed by $|V_{td}V_{ts}| \sim \lambda^5$) which in general is not present in SM extensions, kaon FCNC modes offer a unique window on the flavor structure of such extensions. This argument by itself provides a strong and model-independent motivation to study these modes in the LHC era. Rare kaon decays can elucidate the flavor structure of SM extensions, information that is in general not accessible from high-energy colliders.

The actual "discovery potential" depends on the precision of the prediction for these decays in the SM, the level of constraints from other observables and how well we can measure their branching ratios.

1.3.1 Rare kaon decays in the Standard Model: status and forecast

State-of-the-art predictions (see Ref. [16] and references therein) are summarized in Table 1-2 along with 269 current and expected experimental results. The predictions show our current knowledge of the branching 270 ratio uncertainties: $K^+ \to \pi^+ \nu \bar{\nu}$ at the 10% level, $K_L \to \pi^0 \nu \bar{\nu}$ at the 15% level, and $K_L \to \pi^0 e^+ e^-$ 271 and $K_L \rightarrow \pi^0 \mu^+ \mu^-$ at the 25–30% level. In the charged lepton modes, the uncertainty is dominated 272 by long distance contributions which can be parameterized in terms of the rates of other decays (such as 273 $K_S \to \pi^0 \ell^+ \ell^-$). In the neutrino modes, the irreducible theoretical uncertainty is a small fraction of the total, 274 which is currently dominated by uncertainty in CKM parameters. It is expected that in the next decade 275 progress in lattice QCD and in B meson measurements (LHCb and Belle II) will reduce the uncertainty on 276 both $K \to \pi \nu \bar{\nu}$ modes to the 5% level. Substantial improvements in $K_L \to \pi^0 \ell^+ \ell^-$ will have to rely on 277 lattice QCD computations, requiring evaluation of bi-local operators. Exploratory steps exist but involve 278 new techniques making it hard to forecast the level of uncertainty that can be achieved. Therefore, from a 279 theory perspective, the golden modes remain the $K \to \pi \nu \bar{\nu}$ decays, because they have small long-distance 280

contamination (negligible in the CP violating K_L mode). The $K \to \pi \nu \bar{\nu}$ decay rates, especially in the K_L mode, can be predicted with smaller theoretical uncertainties than other FCNC decay rates involving quarks.

²⁸³ 1.3.2 Beyond the Standard Model physics reach

The Beyond the Standard Model (BSM) reach of rare FCNC kaon decays has received significant attention 284 in the literature, through both explicit model analyses and model-independent approaches based on effective 285 field theory (EFT). In the absence of a clear candidate for the TeV extension of the SM, the case for discovery 286 potential and model-discriminating power can be presented very efficiently in terms of an EFT approach 287 to BSM physics. In this approach, one parameterizes the effects of new heavy particles in terms of local 288 operators which carry dimensionful couplings, suppressed by inverse powers of the heavy new physics mass 289 scale. The important point is that the EFT approach allows us to make statements that apply to classes of 290 models, not just any specific SM extension. In this context, one can ask two important questions: (i) how 291 large of a deviation from the SM can we expect in rare decays from existing constraints? (ii) if a given class 292 of operators dominates, what pattern of deviations from the SM can we expect in various rare kaon decays? 293

Our discussion here parallels the one given in Ref. [18], to which we refer for more details. To leading order in $v_{\rm ew}/\Lambda$ (where $v_{\rm ew} \sim 200$ GeV and Λ is the scale of new physics), six operators can affect the $K \to \pi \nu \bar{\nu}$ decays. Three of these are four-fermion operators and affect the $K \to \pi \ell^+ \ell^-$ decays as well (one of these operators contributes to $K \to \pi \ell \nu$ by SU(2) gauge invariance). The coefficients of these operators are largely unconstrained by other observables, and therefore one can expect sizable deviations from the SM in $K \to \pi \nu \bar{\nu}$ (both modes) and $K \to \pi \ell^+ \ell^-$, depending on the flavor structure of the BSM scenario.

The other three leading operators contributing to $K \to \pi \nu \bar{\nu}$ involve the Higgs field and reduce, after electroweak symmetry breaking, to effective flavor-changing Z-boson interactions, with both left-handed (LH) and right-handed (RH) couplings to quarks. These "Z-penguin" operators (both LH and RH) are the leading effect in many SM extensions, and affect a large number of kaon observables $(K \to \pi \ell^+ \ell^-, \epsilon_K, \epsilon'_K/\epsilon_K)$, and in the case of one operator $K \to \pi \ell \nu$ through SU(2) gauge invariance). Focusing on this class of operators, the relevant part of the effective Lagrangian reads

$$\mathcal{L}_{\text{eff}} \propto \left(\lambda_t C_{\text{SM}} + C_{\text{NP}}\right) \bar{d}_L \gamma_\mu s_L Z^\mu + C_{\text{NP}} d_R \gamma_\mu s_R Z^\mu \,, \tag{1.2}$$

where $\lambda_q = V_{as}^* V_{qd}$ with V_{qp} denoting elements of the CKM matrix, and $C_{\rm SM} \approx 0.8$ encodes the SM 306 contribution to the LH Z-penguin (the RH Z-penguin is highly suppressed in the SM by small quark 307 masses). Assuming dominance of the Z-penguin operators, one can study the expectations for the $K \to \pi \nu \bar{\nu}$ 308 branching ratio for different choices of the effective couplings $C_{\rm NP}$, $C_{\rm NP}$, and address the correlations with 309 other observables. This is illustrated in Fig. 1-2. In this framework, ϵ'_K/ϵ_K provides the strongest constraint 310 on the CP violating mode $K_L \to \pi^0 \nu \bar{\nu}$ [19, 20, 21, 22, 23]. This is illustrated by the green bands in Fig. 1-2, 311 where one can see that the requirement $\epsilon'_K/\epsilon_K \in [0.2, 5](\epsilon'_K/\epsilon_K)_{exp}$ limits deviations in the $K_L \to \pi^0 \nu \bar{\nu}$ to be 312 of $\mathcal{O}(1)$, while leaving room for larger deviations in the CP conserving mode $K^+ \to \pi^+ \nu \bar{\nu}$. The correlation 313 between ϵ'_K/ϵ_K and $K_L \to \pi^0 \nu \bar{\nu}$ can be evaded only if there is a cancellation among the Z-penguin and 314 other contributions to ϵ'_K/ϵ_K . Moreover, we stress that this conclusion holds in all models in which the 315 Z-penguin provides the dominant contribution to $K \to \pi \nu \bar{\nu}$ decays. While this is not true in general, we 316 think this constraint should be one of the drivers of the design sensitivity for $K_L \to \pi^0 \nu \bar{\nu}$ experiments. 317

The number of operators that affect the $K_L \to \pi^0 \ell^+ \ell^-$ ($\ell = e, \mu$) decays is larger than the case of $K \to \pi \nu \bar{\nu}$. Besides (axial-)vector operators resulting from Z- and photon-penguin diagrams, (pseudo-)scalar operators associated with Higgs exchange can play a role [28]. In a model-independent framework:

$$\mathcal{L}_{\text{eff}} \supset C_A Q_A + C_V Q_V + C_P Q_P + C_S Q_S , \qquad (1.3)$$

Community Planning Study: Snowmass 2013

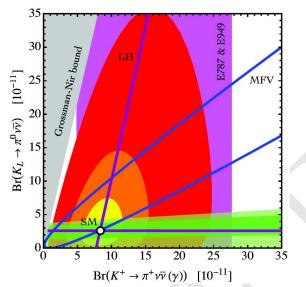


Figure 1-2. Predictions for the $K \to \pi \nu \bar{\nu}$ branching ratios assuming dominance of the Z-penguin operators, for different choices of the effective couplings $C_{\rm NP}, \tilde{C}_{\rm NP}$ [24]. The SM point is indicated by a white dot with black border. The yellow, orange, and red shaded contours correspond to $|C_{\rm NP}, \tilde{C}_{\rm NP}| \leq$ $\{0.5, 1, 2\} |\lambda_t C_{\rm SM}|$, the magenta band indicates the 68% confidence level (CL) constraint on $\mathcal{B}(K^+ \to \pi^+ \nu \bar{\nu} (\gamma))$ from experiment [25], and the gray area is theoretically inaccessible [26]. The blue parabola represents the subspace accessible to MFV models. The purple straight lines represent the subspace accessible in models that have only LH currents, due to the constraint from ϵ_K [27]. The green band represents the region accessible after taking into account the correlation of $K_L \to \pi^0 \nu \bar{\nu}$ with ϵ'_K/ϵ_K : the (light) dark band corresponds to predictions of ϵ'_K/ϵ_K within a factor of (5) 2 of the experimental value, using central values for the hadronic matrix elements as reported in [20] and references therein.

321 with

$$Q_A = (\bar{d}\gamma^\mu s)(\bar{\ell}\gamma_\mu\gamma_5\ell), \quad Q_V = (\bar{d}\gamma^\mu s)(\bar{\ell}\gamma_\mu\ell), \quad Q_P = (\bar{d}s)(\bar{\ell}\gamma_5\ell), \quad Q_S = (\bar{d}s)(\bar{\ell}\ell).$$
(1.4)

In Figure 1-3 we depict the accessible parameter space corresponding to various classes of NP. The blue 322 parabola illustrates again the predictions obtained by allowing only for a contribution $C_{\rm NP}$ with arbitrary 323 modulus and phase. We see that in models with dominance of the LH Z-penguin the deviations in $K_L \rightarrow$ 324 $\pi^0 \ell^+ \ell^-$ are strongly correlated. A large photon-penguin can induce significant corrections in C_V , which 325 breaks this correlation and opens up the parameter space as illustrated by the dashed orange parabola and 326 the yellow shaded region. The former predictions are obtained by employing a common rescaling of $C_{A,V}$, 327 while in the latter case the coefficients $C_{A,V}$ are allowed to take arbitrary values. If besides $Q_{A,V}$ also 328 $Q_{P,S}$ can receive sizable NP corrections a further relative enhancement of $Br(K_L \to \pi^0 \mu^+ \mu^-)$ compared to 329 $Br(K_L \to \pi^0 e^+ e^-)$ is possible. This feature is exemplified by the light blue shaded region that corresponds 330 to the parameter space that is compatible with the constraints on $C_{P,S}$ arising from $K_L \to \mu^+ \mu^-$. Finally, 331 we note that $K_L \to \mu^+ \mu^-$ itself is another FCNC mode of interest, as it is sensitive to different combinations 332 of new physics couplings. The constraining power of $K_L \to \mu^+ \mu^-$ is limited by the current understanding 333 of the dispersive part of the amplitude. Despite this, the mode already provides useful diagnostic power, as 334 in combination with $K \to \pi \nu \bar{\nu}$ can help distinguish among LH or RH coupling of Z and Z' to quarks [29]. 335

Rare kaon decays have been extensively studied within well motivated extensions of the SM, such as supersymmetry (SUSY) [30] and warped extra dimensions (Randall-Sundrum) models [31, 20]. In all cases, deviations from the SM can be sizable and perhaps most importantly the correlations between various rare K decays are essential in discriminating among models. Rare $K \to \pi \nu \bar{\nu}$ experiments can also probe the

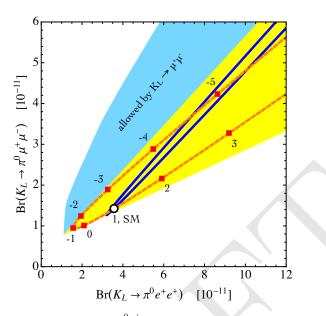


Figure 1-3. Predictions for the $K_L \to \pi^0 \ell^+ \ell^-$ branching ratios assuming different types of NP contributions [24]. The SM point is indicated by a white dot with black border. The blue parabola represents the region accessible by allowing only for $C_{\rm NP}$ with arbitrary modulus and phase. The subspace accessible when $C_{V,A} \neq 0$ is represented by the dashed orange parabola (common rescaling of $C_{A,V}$) and the yellow shaded region (arbitrary values of $C_{A,V}$). The subspace accessible when $C_{S,P} \neq 0$ (compatibly with $K_L \to \mu^+ \mu^-$) is represented by the light blue shaded region.

existence of light states very weakly coupled to the SM appearing in various dark sector models [32], through the experimental signature $K \to \pi +$ (missing energy), and distortions to the pion spectrum.

342 Other modes

Besides the FCNC modes, kaon decays also provide exquisite probes of the charged-current (CC) sector 343 of SM extensions, probing scales of TeV or above. Theoretically, the cleanest probes are (i) the ratio 344 $R_K \equiv \Gamma(K \to e\nu)/\Gamma(K \to \mu\nu)$, which tests lepton universality, scalar, and tensor CC interactions; (ii) the 345 transverse muon polarization P^T_{μ} in the semi-leptonic decay $K^+ \to \pi^0 \mu^+ \nu_{\mu}$, which is sensitive to BSM 346 sources of CP violation in scalar CC operators. In both cases there is a clean discovery window provided 347 by the precise SM theoretical prediction [33] (R_K) and by the fact that in the SM P_{μ}^{T} is generated only 348 by very small and theoretically known final state interactions [34]. Table 1-2 provides a summary of SM 349 predictions for these processes, along with current and projected experimental sensitivities at ongoing or 350 planned experiments. 351

352 1.3.3 Experimental program

Following U.S. termination of a world-class kaon program by 2002, leadership in kaon physics shifted to Europe and Japan. The NA62 experiment at CERN [35] uses a novel in-flight technique to search for $K^+ \to \pi^+ \nu \bar{\nu}$ and will finish commissioning at the end of 2013 and start physics running simultaneous with LHC operations in 2014. The NA62 goal is to measure the $K^+ \to \pi^+ \nu \bar{\nu}$ branching ratio with 10% precision along with a robust and diverse kaon physics program.

The KOTO experiment at JPARC [36] is an in-flight measurement of $K_L^0 \to \pi^0 \nu \bar{\nu}$. Significant experience and a better understanding of the backgrounds to this rare decay mode were obtained in its predecessor E391a. The anticipated experimental sensitivity is a few SM signal events in three years of running with 300 kW of beam power. Commissioning runs were undertaken in 2012 and 2013 and physics runnign started in 2013, but the longer term performance of the experiment will depend upon beam power evolution of the JPARC accelerator.

The TREK Experiment at JPARC [37] will search for T violation in stopped charged kaon decays by measuring the polarization asymmetry in $K^+ \to \pi^0 \mu^+ \nu_\mu$ decays. TREK needs at least 100 kW (proposal assumes 270 kW) for this measurement. While the accelerator is running at lower power, collaborators have proposed a search for lepton flavor universality violation through the measurement of $\Gamma(K \to e\nu)/\Gamma(K \to \mu\nu)$ at the 0.2% level, which will use much of the TREK apparatus and requires only 30 kW of beam power and will be ready to run in 2015. The uncertainty of the JPARC beam power profile and potential conflicts for beamline real estate make the long term future of the TREK experiment unclear.

The KLOE-2 experiment [38] will extend the results of KLOE to improve neutral kaon interference measurements, CPT and quantum mechanics tests and a wide range of measurements of non-leptonic and radiative kaon decays.

The ORKA experiment is proposed to measure $K^+ \to \pi^+ \nu \bar{\nu}$ with 1000 event sensitivity at the Fermilab 375 Main Injector (MI) [39]. After a five year run ORKA will reach a precision of 5% on the branching ratio, 376 which is the expected level of theoretical precision. This high precision measurement would be one of the 377 most incisive probes of quark flavor physics in the coming decade. ORKA is a stopped kaon experiment that 378 builds on the experience of the E787/949 experiments at Brookhaven that observed seven candidate events. 379 Backgrounds, primarily from other kaon decays at branching fractions as much as 10 orders of magnitude 380 larger, have similar signatures to the signal. ORKA takes advantage of the extensive knowledge of background 381 rates and characteristics from E787/E949 by using the same proven experimental techniques. The methods 382 for suppressing backgrounds are well known, as are the background rates and experimental acceptance. 383 Improvements in detector performance are possible due to significant advances in detector technology in the 384 25 years since E787 first ran. The new ORKA detector with beam supplied by the MI running at 95 GeV with 385 moderate duty factor presents an opportunity to extend the E787/E949 approach by two orders of magnitude 386 in sensitivity. The first order of magnitude improvement comes from the substantially brighter source of 387 low energy kaons and the second arises from incremental improvements to the experimental techniques 388 firmly established at BNL. ORKA will observe 210 SM events per year and will make a wide variety of 380 measurements in addition to the $K^+ \to \pi^+ \nu \bar{\nu}$ mode. ORKA will search for and study a range of important 390 reactions involving kaon and pion decays, such as tests of lepton universality, symmetry violations, hidden 391 sector particles, heavy neutrinos and other topics. ORKA will be a world-leading kaon physics experiment. 392 train a new generation of kaon physicists and position the U.S. to move forward to a Project-X kaon program. 393 It is an essential step in developing a robust intensity frontier program in the U.S. at Project-X. 394

The U.S. has an opportunity through ORKA to re-establish a leadership position in kaon physics. ORKA provides a critical path forward by providing a pathway to a strong kaon physics program to anchor a triad of intensity frontier physics at Project-X: neutrinos, muons and kaons.

398 Project-X

A flagship experiment of the Project-X physics program will measure the $K_L^0 \to \pi^0 \nu \bar{\nu}$ branching ratio with 5% precision. This effort will build on the KOTO experience, benefit from the KOPIO initiative [40] and take advantage of the beam power and flexibility provided by Stage 2 of Project-X.

KOPIO proposed to measure $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ with a SM sensitivity of 100 events at the BNL Alternating Gradient Synchrotron (AGS) as part of RSVP (Rare Symmetry Violating Processes) project. The experimental technique and sensitivity were well-developed and extensively reviewed. KOPIO was designed to use a neutral beam at a 42° targeting angle produced by 24 GeV protons from the AGS. The neutral kaons would have an average momentum of 800 MeV/c with a range of 300–1500 MeV/c. A low momentum beam was critical for the Time-Of-Flight (TOF) strategy of the experiment.

The TOF technique is even better matched to the kaon momentum produced by the 3 GeV proton beam at Project-X where the higher momentum tail present in the AGS beam is suppressed. Performance of the TOF strategy was limited by the design bunch width of 200 ps at the AGS. The Project-X beam pulse timing, including target time slewing, is expected to be less than 50 ps and would substantially improve the momentum resolution and background rejection capability of the $K_L^0 \to \pi^0 \nu \bar{\nu}$ experiment driven with the Project-X beam.

⁴¹⁴ The AGS K_L yield per proton is 20 times the Project-X yield; however, the 0.5 mA Project-X proton flux is ⁴¹⁵ 150 times the RSVP goal of 10¹⁴ protons every 5 seconds. Hence the neutral kaon flux at Project-X will be ⁴¹⁶ 8 times the AGS flux goal into the same beam acceptance. The nominal five-year Project-X run is 2.5 times ⁴¹⁷ longer than the KOPIO initiative at the AGS and hence the reach of a Project-X $K_L^0 \to \pi^0 \nu \bar{\nu}$ experiment ⁴¹⁸ would be 20 times greater than RSVP.

A TOF-based $K_L^0 \to \pi^0 \nu \bar{\nu}$ experiment driven by Project-X would be re-optimized for the Project-X K_L 419 momentum spectrum, TOF resolution and corresponding background rejection. It is likely that this opti-420 mization would result in a smaller neutral beam solid angle which would simplify the detector design, increase 421 the acceptance and relax the requirement to tag photons in the fierce rate environment of the neutral beam. 422 Optimizing the performance will probably require a proton pulse train frequency of 20–50 MHz and an 423 individual proton pulse timing width of ~ 20 ps. Based on the E391a and KOTO experience, a careful 424 design of the target and neutral beam channel is required to minimize the neutron halo and to assure target 425 survival in the intense proton beam. The high K_L beam flux, potential of break-through improvements in TOF performance and calorimeter technology support the viability of a $K_L^0 \to \pi^0 \nu \bar{\nu}$ experiment with ~1000 426 427 SM event sensitivity. 428

⁴²⁹ If ORKA [39] observes a significant non-SM result the $K^+ \to \pi^+ \nu \bar{\nu}$ decay mode could be studied with ⁴³⁰ higher statistics with a K^+ beam driven by Project-X. The high-purity, low-momentum K^+ beam designed ⁴³¹ for ORKA could also serve experiments to precisely measure the polarization asymmetry in $K^+ \to \pi^0 \mu^+ \nu_{\mu}$ ⁴³² decays and to continue the search for lepton flavor universality violation through the measurement of $\Gamma(K \to \mu\nu)/\Gamma(K \to \mu\nu)$ at high precision.

⁴³⁴ Depending upon the outcome of the TREK experiment at JPARC, a T violation experiment would be an ⁴³⁵ excellent candidate for Project-X, as would a multi-purpose experiment dedicated to rare modes that involve ⁴³⁶ both charged and neutral particles in the final state. This experiment might be able to pursue $K_L \to \pi^0 \ell^+ \ell^-$ ⁴³⁷ as well as many other radiative and leptonic modes. The kaon physics program at Project-X could be very ⁴³⁸ rich indeed.

439 1.3.4 Conclusions

Kaon decays are extremely sensitive probes of the flavor and CP-violating sector of any SM extension. The $K \to \pi \nu \bar{\nu}$ golden modes have great discovery potential: (i) sizable, $\mathcal{O}(1)$, deviations from the SM are possible; (ii) even small deviations can be detected due to the precise theoretical predictions. Next generation searches should aim for a sensitivity level of 10^3 SM events (few %) in both K^+ and K_L modes, so as to maximize discovery potential.

We foresee searches for both $K \to \pi \nu \bar{\nu}$ modes as flagship measurements of a reinvigorated US-led kaon program. As summarized in Table 1-2, through ORKA and Project-X this program has the opportunity to pursue a broad set of measurements, exploring the full discovery potential and model-discrimination power of kaon physics.

⁴⁴⁹ 1.4 Report of the *B*-Physics Task Force

450 1.4.1 Physics Motivation: searches for BSM physics

Rare B physics processes are sensitive to New Physics (NP) because the heavy particles can contribute 451 through virtual corrections to the effective weak Hamiltonian. In this way one can, e.g., probe extended 452 Higgs sectors, test for the presence of new gauge interactions or for extended matter content such as the ones 453 encountered in supersymmetric models. The sensitivity to NP depends on how large the flavor violating 454 couplings are. For instance, in the most conservative case of Minimal Flavor Violation (MFV) with new 455 particles only contributing in the loops, the rare B processes can probe mass scales of roughly $\sim \mathcal{O}(\text{TeV})$ 456 with the next generation super flavor factory. In the case of general flavor violation with $\mathcal{O}(1)$ off-diagonal 457 couplings, on the other hand, one probes mass scales of $\mathcal{O}(10^3 \,\text{TeV})$ [1]. Because the dependence on new 458 particle masses and (flavor violating) couplings is different than in the on-shell production, the NP searches 459 at LHCb and Belle II are also complementary to the high p_T NP searches at ATLAS and CMS. 460

For future B physics program especially interesting observables are the ones that have vanishingly small or 461 systematically improvable uncertainties. An important input is provided by measurements of the standard 462 CKM unitarity triangle. The angle γ and modulus $|V_{ub}|$ are determined from tree-level processes and thus less 463 prone to contributions from NP. They will provide the SM "reference" determination of the CKM unitarity 464 triangle (in effect its apex, the values of $\bar{\rho}$ and $\bar{\eta}$). $|V_{ub}|$ is measured from inclusive and exclusive $b \to u l \nu$ 465 processes. There is an on-going effort to improve the theory predictions using both the continuum methods 466 and lattice QCD, with a factor of a few improvements on the errors potentially feasible. For instance, the 467 present theory error on $|V_{ub}|$ from exclusive $B \to \pi l \nu$ can be reduced from present 8.7% to 2% by 2018 [41]. 468 The theoretical uncertainties in the measurement of γ from $B \to DK$ decays is even smaller. All the required 469 hadronic matrix elements can be measured, because of the cascade nature of the $B \to DK$, $D \to f$ decay, if 470 enough final states f are taken into account. The irreducible theoretical errors thus enter only at the level of 471 one loop electroweak corrections and is below $\mathcal{O}(10^{-6})$ [42]. The present experimental errors are $\pm 12^{\circ}$ from 472 the average of BABAR and Belle measurements. The LHCb has recently matched this precision. The errors 473 are statistics limited and will be substantially decreased in the future. 474

The tree-level determinations of $\bar{\rho}$ and $\bar{\eta}$ can then be compared with the measurements from loop induced

- ⁴⁷⁶ FCNCs, for instance with the time dependent CP asymmetry in $B \rightarrow J/\psi K_S$ and related modes, determining
- 477 the angle β . With improved theoretical control BSM physics can be constrained or even discovered. NP
- could also enter in the $B_s \overline{B}_s$ mixing. In the SM the mixing phase is small, suppressed by λ^2 compared to

⁴⁷⁹ β . The corresponding time-dependent CP asymmetry in the $b \to c\bar{c}s$ dominated decays, such as $B_s \to J/\psi \phi$, ⁴⁸⁰ is thus in the SM $\beta_s^{(SM)} = 0.0182 \pm 0.0008$. The LHCb result $\beta_s = -0.035 \pm 0.045$ [43] is consistent with ⁴⁸¹ the SM expectation, albeit within relatively large statistical errors. Since the errors on the SM prediction ⁴⁸² are very small, future significant improvements on the measurement of β_s will directly translate to a better ⁴⁸³ constraint on BSM physics.

Another important search for NP is to compare the time-dependent CP asymmetries of penguin dominated $b \rightarrow q\bar{q}s$ processes with the tree dominated $b \rightarrow c\bar{c}s$ decays. Observables that probe this are the difference of CP asymmetries $S_{\psi K_S} - S_{\phi K_S}$, $S_{\psi K_S} - S_{\eta' K_S}$, ... in B_d decay, and $S_{\psi\phi} - S_{\phi\phi}$ in B_s decay.

In fact, the list of interesting observables in B physics is very long. One could emphasize in particular the rare 487 B decays with leptons in the final state. The $B_s \to \ell^+ \ell^-$ decay is especially interesting for SUSY searches 488 in view of the fact that these are $(\tan \beta)^6$ enhanced. The LHCb has presented first evidence of this decay, with $\mathcal{B}(B_s \to \mu^+\mu^-) = (3.2^{+1.5}_{-1.2}) \times 10^{-9}$ [44] consistent with the SM prediction $(3.23 \pm 0.27) \times 10^{-9}$ [45]. 489 490 This puts a nontrivial constraint on the large tan β region of MSSM, favored by the measured Higgs mass for 491 the case of TeV scale squarks. The theoretical errors on the SM prediction are still a factor of a few below 492 the experimental ones, making more precise measurements highly interesting. With the LHCb upgrade the 493 search for $B_d \to \ell^+ \ell^-$ may also get near the SM level. Rare decays involving a $\nu \bar{\nu}$ pair are theoretically very 494 clean, and the next generation of e^+e^- machines should reach the SM level in $B \to K^{(*)}\nu\bar{\nu}$; the current 495 constraints are an order of magnitude weaker. There is also a long list of interesting measurements in 496 $b \to s\gamma$ and $b \to s\ell^+\ell^-$ mediated inclusive and exclusive decays, CP asymmetries, angular distributions, 497 triple product correlations, etc., which will be probed much better in the future. The $s \leftrightarrow d$ processes, with 498 lower SM rates, will provide many other challenging measurements and opportunities to find NP. Rare B 499 decays can also be used as probes for "hidden sector" particle searches, for lepton flavor violation, and for 500 baryon number violating processes. 501

There are also some intriguing deviations from the SM in the current data. The DO collaboration measured the CP-violating dilepton asymmetry to be 4σ away from zero, $A_{\rm SL}^b = (7.87 \pm 1.96) \times 10^{-3} \approx 0.6 A_{\rm SL}^d + 0.4 A_{\rm SL}^s$ [46]. The measured semileptonic asymmetry is a mixture of B_d and B_s ones, where $A_{\rm SL} \simeq 2(1-|q/p|)$ in each case measures the mismatch of the CP and mass eigenstates. In the SM, (1 - |q/p|) is modelindependently suppressed by m_b^2/m_W^2 , with an additional m_c^2/m_b^2 suppression in the SM, which NP may violate [47]. Since the DO result allows plenty of room for NP, it will be important for LHCb and Belle II to clarify the situation. LHCb has recently measured $A_{\rm SL}^s = (-2.4 \pm 5.4 \pm 3.3) \times 10^{-3}$ [48] which complements $A_{\rm SL}^d$ measured at e^+e^- B factories. Further improvement in experimental errors on both quantities is needed.

Another interesting anomaly is the hint of the flavor universality violation in $B \to D^{(*)}\tau\nu$ decays observed by BABAR [49] which differ from the SM prediction expected from the $B \to D^{(*)}\ell\nu$ rates by 3.4 σ . Combined with the slight excess of $\mathcal{B}(B \to \tau\nu)$ over the SM the measurements can be explained using charged Higgs exchange, e.g., in the two Higgs doublet model, but with nontrivial flavor structure [50]. The Minimal Flavor Violation hypothesis is not preferred. To settle the case it will require larger data sets at the future e^+e^- B factories (and measuring the $B \to \mu\bar{\nu}$ mode as well).

Any of the above measurements could lead to a discovery of New Physics. However, the real strength of the ⁵¹⁶ *B* physics program is that a pattern of modifications in different measurements that show or do not show ⁵¹⁸ deviations from the SM can zoom in on the correct NP model. This will provide complementary information ⁵¹⁹ to the on-shell searches at the LHC. Further information will also be provided by the searches for lepton ⁵²⁰ flavor violation in charged lepton decays, e.g., $\tau \to \mu \gamma$ and $\tau \to 3\mu$.

⁵²¹ 1.4.2 Physics potential of e^+e^- experiments: Belle II

The spectacular successes of the *B*-factory experiments Belle and *BABAR* highlight the advantages of $e^+e^$ collider experiments:

• Running on the $\Upsilon(4S)$ resonance produces an especially clean sample of $B^0\overline{B}^0$ pairs in a quantum correlated 1⁻⁻ state. The low background level allow reconstruction of final states containing γ 's and particles decaying to γ 's: π^0 , ρ^{\pm} , η , η' , etc. Neutral K_L^0 mesons are also efficiently reconstructed. The quantum correlation allows the decay of one *B* to tag the flavor of the other.

• Due to low track multiplicities and detector occupancy, the reconstruction efficiency is high and the trigger bias is low. This substantially reduces corrections and systematic uncertainties in many types of measurements, e.g., Dalitz plot analyses.

• By utilizing asymmetric beam energies, the Lorentz boost β of the e^+e^- system can be made large enough such that a *B* or *D* meson travels an appreciable distance before decaying. This allows precision measurements of lifetimes, mixing parameters, and CP violation (CPV). Note that measurement of the *D* lifetime provides a measurement of the mixing parameter y_{CP} , while measurement of the *B* lifetime (which is already well measured) allows one to determine the decay time resolution function from data.

• Since the absolute delivered luminosity is measured with Bhabha scattering, an e^+e^- experiment measures *absolute* branching fractions. These are complementary to *relative* branching fractions measured at hadron colliders, and in fact are used to normalize the relative measurements.

• Since the initial state is completely known, one can perform "missing mass" analyses, i.e., infer the existence of new particles via energy/momentum conservation rather than reconstructing their final states. By fully reconstructing a *B* decay in one hemisphere of the detector, inclusive decays such as $B \rightarrow X_s \ell^+ \ell^-$, $X_s \gamma$ can be measured in the "opposite" hemisphere.

• In addition to producing large samples of B and D decays, an e^+e^- machine produces large sample of τ leptons. This allows one to measure rare τ decays and search for forbidden τ decays with a high level of background rejection.

To extend this physics program beyond the Belle and BABAR experiments, the KEKB e^+e^- accelerator 546 at the KEK laboratory in Japan will be upgraded to "SuperKEKB," and the Belle experiment will be 547 upgraded to "Belle II." The KEKB accelerator achieved a peak luminosity of $2.1 \times 10^{34} \,\mathrm{cm}^{-2} \mathrm{s}^{-1}$, and the 548 Belle experiment recorded a total integrated luminosity of 1040 fb⁻¹ (just over 1.0 ab^{-1}). The SuperKEKB 549 accelerator plans to achieve a luminosity of $8 \times 10^{35} \,\mathrm{cm}^{-2} \mathrm{s}^{-1}$, and the Belle II experiment plans to record 550 50 ab⁻¹ of data by 2022. As $\sigma(e^+e^- \to b\bar{b}) \approx 1.1$ nb at the $\Upsilon(4S)$ resonance, this data sample will contain 551 $5 \times 10^{10} B\overline{B}$ pairs. Such a large sample will improve the precision of time-dependent CPV measurements 552 and the sensitivity of searches for rare and forbidden decays. Systematic errors should also be reduced, as 553 control samples from which many are calculated will substantially increase. 554

A discussion of the complete physics program of Belle II is beyond the scope of this summary. Here we touch upon only a few highlights. More complete writeups can be found in Refs. [51] and [52]; the latter was written in the context of the proposed — but declined — SuperB experiment in Italy. The expected sensitivity of Belle II in 50 fb⁻¹ of data for various topical *B* decays is listed in Table 1-3.

As mentioned above, a main strength of a *B* factory experiment is the ability to make precision measurements of CP violation, and this capability will be exploited to search for NP sources of CPV. The difference between

 B^0 and \overline{B}^0 decay rates to a common self-conjugate state is sensitive to both direct CPV (i.e., occurring in

Observable	SM theory	Current measurement	Belle II
Observable	uncertainty	(early 2013)	$(50 {\rm ab}^{-1})$
$\overline{S(B \to \phi K^0)}$	0.68	0.56 ± 0.17	± 0.03
$S(B o \eta' K^0)$	0.68	0.59 ± 0.07	± 0.02
α from $B \to \pi \pi, \rho \rho$		$\pm 5.4^{\circ}$	$\pm 1.5^{\circ}$
γ from $B \to DK$		$\pm 11^{\circ}$	$\pm 1.5^{\circ}$
$S(B \to K_S \pi^0 \gamma)$	< 0.05	-0.15 ± 0.20	± 0.03
$S(B o ho \gamma)$	< 0.05	-0.83 ± 0.65	± 0.15
$A_{\rm CP}(B \to X_{s+d} \gamma)$	< 0.005	0.06 ± 0.06	± 0.02
$A^d_{ m SL}$	-5×10^{-4}	-0.0049 ± 0.0038	± 0.001
$\overline{\mathcal{B}(B \to \tau \nu)}$	1.1×10^{-4}	$(1.64\pm 0.34)\times 10^{-4}$	$\pm 0.05 \times 10^{-4}$
$\mathcal{B}(B o \mu u)$	4.7×10^{-7}	$< 1.0 \times 10^{-6}$	$\pm 0.2 \times 10^{-7}$
$\mathcal{B}(B \to X_s \gamma)$	3.15×10^{-4}	$(3.55\pm0.26) imes10^{-4}$	$\pm 0.13 \times 10^{-4}$
$\mathcal{B}(B \to X_s \ell^+ \ell^-)$	1.6×10^{-6}	$(3.66\pm 0.77) imes 10^{-6}$	$\pm 0.10 \times 10^{-6}$
$\mathcal{B}(B o K \nu \overline{\nu})$	$3.6 imes 10^{-6}$	$< 1.3 \times 10^{-5}$	$\pm 1.0 \times 10^{-6}$
$A_{\rm FB}(B \to K^* \ell^+ \ell^-)_{q^2 < 4.3 {\rm GeV}^2}$	-0.09	0.27 ± 0.14	± 0.04
$s_0 A_{\rm FB}(B^0 \to K^{*0} \ell^+ \ell^-)$	0.16	0.029	0.008
$ V_{ub} $ from $B \to \pi \ell^+ \nu ~(q^2 > 16 {\rm GeV^2})$	9% ightarrow 2%	11%	2.1%

Table 1-3. The expected reach of Belle II in 50 ab^{-1} of data for various topical *B* decay measurements. For comparison, also listed are the Standard Model expectation and the current best experimental results. For $|V_{ub}|$ we list the fractional error.

the B^0 and \overline{B}^0 decay amplitudes), and indirect CPV from interference between the $B \to f$ decay and 562 $B \to \overline{B}^0 \to f$ mixing amplitudes. The indirect CPV was originally done at Belle and BABAR for all-charged 563 final states such as $J/\psi K^0$ [53, 54] (see Fig. 1-4, left) and $\pi^+\pi^-$ [55, 56]; at Belle II, this measurement will 564 be extended with good statistics to more challenging final states such as $B^0 \to K_S^0 K_S^0$ (Fig. 1-4, left, shows 565 a first measurement by Belle), $B^0 \to K^0 \pi^0$, and $B^0 \to X_{s+d} \gamma$. The last mode proceeds via electromagnetic 566 $b \to s\gamma$ and $b \to d\gamma$ penguin amplitudes, where X_{s+d} represents the hadronic system in these decays. In 567 a fully inclusive measurement, the γ is measured but X_{s+d} is not reconstructed. In the Standard Model 568 (SM) there is a robust expectation that direct CP violation is negligible, i.e., the decay rates for B and \overline{B} to 569 $X_{s+d}\gamma$ are equal. A measured difference would be a strong indication of NP, and differences of up to 10% 570 appear in some non-SM scenarios. The best measurement with existing B-factory data is consistent with no 571 difference and has a 7% absolute error [57]. Belle II should reduce this uncertainty to below 1%. 572

Both Belle and BABAR used the $b \to c\bar{c}s$ "tree" mode $B^0 \to J/\psi K^0$ to measure the phase β of the CKM 573 unitary triangle to high precision: $\sin(2\beta) = 0.665 \pm 0.022$ [58]. However, this phase can also be measured in 574 $b \to s\bar{s}s$ "loop" decays such as $B^0 \to \phi K^0$ and $B^0 \to \eta' K^0$. Since virtual NP contributions could compete 575 with the SM loop diagrams, these modes are sensitive to NP. Comparing the values of $\sin(2\beta)$ measured 576 in $b \to c\bar{c}s$ and in $b \to s\bar{s}s$ processes thus provides a way to search for NP. The decay $B^0 \to \eta' K^0$ is the 577 most precisely measured $b \to s\bar{s}s$ mode; the value of $\sin(2\beta)$ obtained is 0.59 ± 0.07 [58], about 1.2σ lower 578 than that measured in $B^0 \to J/\psi K^0$ decays. Belle II is expected to reduce this error by almost an order of 579 magnitude, making the test much more sensitive. 580

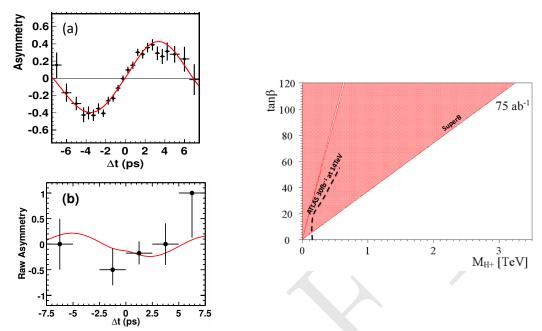


Figure 1-4. Left: Belle measurements of the time-dependent CP asymmetry versus Δt for (a) $B \to J/\psi K^0$ and (b) $B \to K_S^0 K_S^0$. The parameter $\sin(2\beta)$ is determined from the amplitude of the oscillations. Belle II should obtain statistics for $B \to K_S^0 K_S^0$ (and other loop-dominated modes) comparable to those obtained by Belle for $B \to J/\psi K^0$. Right: The expected constraint in m_H vs. $\tan \beta$ parameter space for a Type II Higgs doublet model that would result from 75 ab^{-1} of data at a super-B-factory. For comparison, also shown is the expected constraint from ATLAS in 30 fb⁻¹ of data.

The $B^0 \to K^0 \pi^0$ CP asymmetry is an important component of a sum rule which holds in the isospin limit [59]

$$\mathcal{A}_{K^{+}\pi^{-}} \frac{\mathcal{B}_{K^{+}\pi^{-}}}{\tau_{B^{0}}} + \mathcal{A}_{K^{0}\pi^{+}} \frac{\mathcal{B}_{K^{0}\pi^{+}}}{\tau_{B^{+}}} = 2\mathcal{A}_{K^{+}\pi^{0}} \frac{\mathcal{B}_{K^{+}\pi^{0}}}{\tau_{B^{+}}} + 2\mathcal{A}_{K^{0}\pi^{0}} \frac{\mathcal{B}_{K^{0}\pi^{0}}}{\tau_{B^{0}}},$$
(1.5)

where \mathcal{A} denotes a CP asymmetry, \mathcal{B} a branching fraction, and τ a lifetime. This sum rule is thought to be accurate to a few percent precision and provides a robust test of the SM. The limitation of the test is the precision of $\mathcal{A}_{K^0\pi^0}$, which is difficult to measure and currently known to only ~14% precision [60]. At Belle II this is expected to be reduced to ~3% precision, greatly improving the sensitivity of Eq. (1.5) to NP.

Numerous rare B decays that were observed with low statistics by Belle and BABAR or not at all will become 586 accessible at Belle II. One example is $B^+ \to \tau^+ \nu$, which in the SM results from a W-exchange diagram and has an expected branching fraction of $(0.76^{+0.10}_{-0.06}) \times 10^{-4}$ [61]. This mode is sensitive to supersymmetric 587 588 models and others that predict the existence of a charged Higgs. The final state contains multiple neutrinos 589 and thus is feasible to study only at an e^+e^- experiment. The current average branching fraction from Belle 590 and BABAR is $(1.15\pm0.23)\times10^{-4}$ [62, 63, 64, 65], somewhat higher than the SM expectation. Belle II should 591 reduce this error to about 0.04×10^{-4} . The contribution of a charged Higgs boson within the context of a 592 Type II Higgs doublet model (e.g., which is also the tree level Higgs sector of the Minimal Supersymmetric 593 Model) would increase the branching fraction above the SM prediction by a factor $1 - (m_B^2/m_H^2) \tan^2 \beta$, 594 where m_H is the mass of the charged Higgs and $\tan\beta$ is the ratio of vacuum expectation values of up-type 595 and down-type Higgses. This relation can be used in conjunction with the measured value of the branching 596 fraction to constrain m_H and $\tan\beta$. The expected constraint from a B-factory experiment with 75 ab⁻¹ of 597 data is shown in Fig. 1-4 (right). One sees that a large region of phase space is excluded. For $\tan \beta \gtrsim 60$, 598 the range $m_H < 2 \text{ TeV}/c^2$ is excluded. 599

Other interesting processes include $b \to s\ell^+\ell^-$ and $b \to d\ell^+\ell^-$, with $\ell = e$ or μ . These are also sensitive to 600 NP via loop diagrams. Belle II will reconstruct a broad range of exclusive final states such as $B \to K^{(*)}\ell^+\ell^-$, 601 from which one can determine CP asymmetries, forward-backward asymmetries, and isospin asymmetries 602 (i.e., the asymmetry between $B^+ \to K^{(*)+}\ell^+\ell^-$ and $B^0 \to K^{(*)0}\ell^+\ell^-$). Belle II will also measure inclusive 603 processes such as $B \to X_{s+d} \ell^+ \ell^-$, for which theoretical predictions have less uncertainty than those for 604 exclusive processes. By running on the $\Upsilon(5S)$ resonance, Belle II can study B_s^0 decays. Topical decay modes 605 include $B_s^0 \to D_s^{*+} D_s^{*-}$, $D_s^{*+} \rho^{-}$, and $B_s^0 \to \gamma \gamma$, all of which are difficult to trigger on and reconstruct in a 606 hadronic environment. 607

⁶⁰⁸ The SuperKEKB project at KEK is well underway. Commissioning of the accelerator is expected to begin ⁶⁰⁹ in 2015. The high luminosity (8×10^{35} cm⁻²s⁻¹, 40 times larger than KEKB) results mainly from a smaller ⁶¹⁰ β^* function and reduced emittance. As a result, the vertical beam spread at the interaction point will shrink ⁶¹¹ from ~2 μ m at KEKB to ~60 nm at SuperKEKB. In addition, the beam currents will be approximately ⁶¹² doubled, and the beam-beam parameter will be increased by 50%.

The Belle II detector will be an upgraded version of the Belle detector that can handle the increased 613 backgrounds associated with higher luminosity. The inner vertex detector will employ DEPleted Field Effect 614 (DEPFET) pixels located inside a new silicon strip tracker employing the APV25 ASIC (developed for 615 CMS) to handle the large rates. There will also be a new small-cell drift chamber. The particle identification 616 system will consist of an "imaging-time-of-propagation" (iTOP) detector in the barrel region, and an aerogel-617 radiator-based ring-imaging Cherenkov detector in the forward endcap region. The iTOP operates in a 618 similar manner as BABAR's DIRC detector, except that the photons are focused with a spherical mirror onto 619 a finely segmented array of multi-channel-plate (MCP) PMTs. These MCP PMTs provide precise timing. 620 which significantly improves the discrimination power between pions and kaons over that provided by imaging 621 alone. The CsI(Tl) calorimeter will be retained but instrumented with waveform sampling readout. The 622 innermost layers of the barrel K_L^0/μ detector, and all layers of the endcap K_L^0/μ detector, will be upgraded 623 to use scintillator in order to accommodate the higher rates. Belle II should be ready to roll in by the spring 624 of 2016 after commissioning of SuperKEKB is completed. The US groups on Belle II are focusing their 625 efforts on the iTOP and K_L^0/μ systems. 626

627 1.4.3 Physics potential of hadronic experiments

628 LHCb and its upgrade

Hadron colliders have great potential for studying the decays of particles containing charm and bottom 629 quarks. The production cross sections are quite large and the machine luminosities are very high, so more 630 than 100 kHz of b-hadrons within the detector acceptance can be produced per second even at reduced 631 LHC luminosities $(4 \times 10^{32} \text{ cm}^{-2} \text{s}^{-1})$. This is a much higher production rate than can be achieved even in 632 the next generation $e^+e^- B$ factories. All species of b-flavored hadrons, including B_s , B_c , and b baryons, 633 are produced. However, compared to $e^+e^- b$ and charm factories, the environment is much more harsh for 634 experiments. At hadron colliders, the b quarks are accompanied by a very high rate of background events; 635 they are produced over a very large range of momenta and angles; and even in b-events of interest there is a 636 complicated underlying event. The overall energy of the center of mass of the hard scatter that produces the 637 b quark, which is usually from the collision of a gluon from each beam particle, is not known, so the overall 638 energy constraint that is so useful in e^+e^- colliders is not available. These features translate into challenges 639 in triggering, flavor tagging, photon detection and limit the overall efficiency. 640

The CDF and DO experiments at the Fermilab Tevatron demonstrated that these problems could be suc-641 cessfully addressed using precision silicon vertex detectors and specialized triggers. While these experiments 642 were mainly designed for high- p_T physics, they nevertheless made major contributions to bottom and charm 643 physics [66, 67]. 644

The LHC produced its first collisions at 7 TeV center of mass energy at the end of March 2010. The b cross 645 section at the LHC is $\sim 300\mu b$, a factor of three higher than at the Tevatron and approximately 0.5% of the 646 inelastic cross section. When the LHC reaches its design center of mass energy of 14 TeV in 2015, the cross 647 section will be a factor of two higher. 648

The LHC program features for the first time at a hadron collider a dedicated B-physics experiment, 649 LHCb [68]. LHCb covers the forward direction from about 10 mr to 300 mr with respect to the beam 650 line. B hadrons in the forward direction are produced by collisions of gluons of unequal energy, so that 651 the center of mass of the collision is Lorentz boosted in the direction of the detector. Because of this, the 652 b-hadrons and their decay products are produced at small angles with respect to the beam and have momenta 653 ranging from a few GeV/c to more than a hundred GeV/c. Because of the Lorentz boost, even though the 654 angular range of LHCb is small, its coverage in pseudorapidity is from about 2 to about 5 and both b hadrons 655 travel in the same direction, making b flavor tagging possible. With the small angular coverage, LHCb can 656 stretch out over a long distance along the beam without becoming too large transversely. A silicon microstrip 657 vertex detector (VELO) only 8 mm from the beam provides precision tracking that enables LHCb to separate 658 weakly decaying particles from particles produced at the interaction vertex. This allows the measurement of 659 lifetimes and oscillations due to flavor mixing. A 4 Tm dipole magnet downstream of the collision region, in 660 combination with the VELO, large area silicon strips (TT) placed downstream of the VELO but upstream of 661 the dipole, and a combination of silicon strips (IT) and straw tube chambers (OT) downstream of the dipole 662 provides a magnetic spectrometer with excellent mass resolution. There are two Ring Imaging Cherenkov 663 counters, one upstream of the dipole and one downstream, that together provide $K-\pi$ separation from 2 664 to 100 GeV/c. An electromagnetic calorimeter (ECAL) follows the tracking system and provides electron 665 triggering and π^0 and γ reconstruction. This is followed by a hadron calorimeter (HCAL) for triggering on 666 hadronic final states. A muon detector at the end of the system provides muon triggering and identification. 667

LHCb has a very sophisticated trigger system [69] that uses hardware at the lowest level (L0) to process the 668 signals from the ECAL, HCAL and muon systems. The L0 trigger reduces the rate to ~ 1 MHz followed by 669 the High Level Trigger (HLT), a large computer cluster, that reduces the rate to ~ 3 kHz for archiving to 670 tape for physics analysis. LHCb is able to run at a luminosity of 4.0×10^{32} cm⁻²s⁻¹. This is much smaller 671 than the current peak luminosity achieved by the LHC and only a few percent of the LHC design luminosity. 672 The luminosity that LHCb can take efficiently is currently limited by the 1 MHz bandwidth between the 673 Level 0 trigger system and the trigger cluster. Therefore, the physics reach of LHCb is determined by the 674 detector capabilities and not by the machine luminosity. In fact, LHC implemented a "luminosity leveling" 675 scheme in the LHCb collision region so that LHCb could run at its desired luminosity throughout the store 676 while the other experiments, CMS and ATLAS, could run at higher luminosities. This mode of running will 677 continue until 2017 when a major upgrade [70, 71] of the LHCb trigger and parts of the detector and front end 678 electronics will increase the bandwidth to the HLT, increase archiving rate to 20 kHz, and permit operation 679 at a factor of 10 higher luminosity. Several subdetectors will be rebuilt for more robust performance at 680 higher luminosities, including VELO (pixels), TT (finer strips), IT+OT (technology to be soon decided) and 681 RICH (redesigned optics, MaPMTs). 682

There have been three runs of the LHC. In the first "pilot" run in 2010, LHCb recorded 35 pb^{-1} , which 683 was enough to allow it to surpass in precision many existing measurements of B decays. In 2011, the LHC 684 delivered more than 5 fb⁻¹ to CMS and ATLAS. Since this luminosity was more than LHCb was designed to 685 handle, the experiment ran at a maximum luminosity that was 10% of the LHC peak luminosity. The total 686 integrated luminosity was about 1 fb⁻¹. In 2012 LHC delivered 20 fb⁻¹ to CMS and ATLAS with additional 687

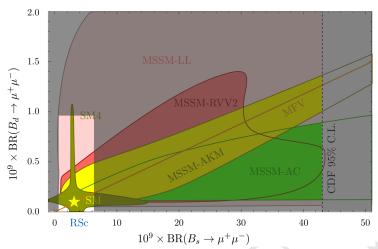


Figure 1-5. Correlation between the branching ratios of $B_s^0 \to \mu^+ \mu^-$ and $B_d^0 \to \mu^+ \mu^-$ in various models. The SM point is marked by a star. From Ref. [76] with the 1.1 fb⁻¹ LHCb result [44] superimposed.

⁶⁶⁸ 2 fb⁻¹ collected by LHCb. Until the LHCb upgrade is installed in the long shutdown planned in 2018, LHCb ⁶⁶⁹ plans to run at a luminosity of 4.0×10^{32} cm⁻²s⁻¹. Between now and then, LHCb will accumulate about ⁶⁹⁰ 1–2 fb⁻¹ per operating year, so a total of about 6.5 fb⁻¹ will be obtained. The sensitivity will increase by ⁶⁹¹ more than this because the LHC will run at 14 TeV, with about a factor of two higher *B* cross section. After ⁶⁹² the upgrade is installed, LHCb will integrate about 5 fb⁻¹ per year, so that about 50 fb⁻¹ will be obtained ⁶⁹³ over the decade following the upgrade installation.

⁶⁹⁴ The decay $B_s \to J/\psi \phi$ has been used to measure the CKM angle $\phi_s (\equiv -2\beta_s)$ [43]. The result, using also ⁶⁹⁵ the decay mode $B_s \to J/\psi f_0$ [72] first established by LHCb [73], is $\phi_s = 0.01 \pm 0.07 \pm 0.01$ rad [43]. The ⁶⁹⁶ difference in the width of the CP-even and CP-odd B_s mesons is $\Delta \Gamma_s = (0.106 \pm 0.011 \pm 0.007)$ ps⁻¹. These ⁶⁹⁷ results are consistent with the SM, resolving a slight tension with earlier measurements from the Tevatron, ⁶⁹⁸ which deviated somewhat from the SM predictions. However, the experimental uncertainty on ϕ_s is still a ⁶⁹⁹ factor of 40 larger than that on the SM prediction, therefore improved measurements will probe higher mass ⁷⁰⁰ scales of possible NP contributions.

A discussion of a few out of many LHCb results now follows. The rare decay $B_s \to \mu^+ \mu^-$ is predicted in the SM to have a branching fraction $(3.23 \pm 0.27) \times 10^{-9}$ [45]. A higher or lower branching fraction would be an indicator for NP. LHCb has presented first evidence of this decay based on 1.1 fb⁻¹ of data, with $\mathcal{B}(B_s \to \mu^+ \mu^-) = (3.2^{+1.5}_{-1.2}) \times 10^{-9}$ [44] consistent with the SM prediction. At present the measurements from the CMS (5 fb⁻¹) [74] and ATLAS (2.4 fb⁻¹) [75] have lower sensitivity and lead to upper limits only. LHCb has also set an upper limit on $\mathcal{B}(B_d \to \mu^+ \mu^-) < 0.94 \times 10^{-9}$ (95% C.L.). Together with the result for $\mathcal{B}(B_d \to \mu^+ \mu^-)$, the LHCb measurements impose stringent constraints on SUSY models as illustrated in Fig. 1-5. Further increase in statistics will probe even higher energy scales.

LHCb has also produced results on the key decay $B^0 \to K^{*0} \mu^+ \mu^-$ (1.1 fb⁻¹) [77] that could reveal evidence 709 for NP. One of the interesting observables is the forward-backward asymmetry of the μ^- relative to the 710 direction of the parent B^0 meson in the dimuon center of mass vs. q^2 (dimuon invariant mass). The SM 711 prediction crosses zero within a well-determined narrow region of q^2 , due to the interference between the SM 712 box and electroweak penguin diagrams. NP can remove the crossover or displace its location. Indications 713 from low statistics at Belle, BABAR, and CDF seemed to indicate that this might be happening. The new 714 LHCb results are the most precise so far, are in good agreement with the SM within errors, which however 715 can be significantly reduced with the LHCb upgrade. Many other observables sensitive to NP have been also 716

Observable	SM theory	Precision	LHCb	LHCb Upgrade
Observable	uncertainty	as of 2013	(6.5 fb^{-1})	(50 fb^{-1})
$2\beta_s(B_s \to J/\psi\phi)$	~ 0.003	0.09	0.025	0.008
$\gamma(B \to D^{(*)}K^{(*)})$	$< 1^{\circ}$	8°	4°	0.9°
$\gamma(B_s \to D_s K)$	$< 1^{\circ}$		$\sim 11^{\circ}$	2°
$\beta(B^0 \to J/\psi K_S^0)$	small	0.8°	0.6°	0.2°
$ \frac{2\beta_s^{\text{eff}}(B_s \to \phi\phi)}{2\beta_s^{\text{eff}}(B_s \to K^{*0}\bar{K}^{*0})} \\ \frac{2\beta_s^{\text{eff}}(B_s \to \phi\gamma)}{2\beta_s^{\text{eff}}(B^0 \to \phi K_S^0)} $	0.02	1.6	0.17	0.03
	< 0.02		0.13	0.02
	0.2%		0.09	0.02
	0.02	0.17	0.30	0.05
$A^s_{ m SL}$	0.03×10^{-3}	6×10^{-3}	1×10^{-3}	0.25×10^{-3}
$\mathcal{B}(B_s \to \mu^+ \mu^-)$	8%	42%	15%	5%
$\mathcal{B}(B^0 \to \mu^+ \mu^-) / \mathcal{B}(B_s \to \mu^+ \mu^-)$	5%	-	$\sim 100\%$	${\sim}35\%$
$s_0 A_{\rm FB}(B^0 \to K^{*0} \mu^+ \mu^-)$	7%	18%	6%	2%

Table 1-4. Sensitivity of LHCb to key observables. The current sensitivity (based on 1–3 fb⁻¹, depending on the measurement) is compared to that expected after 6.5 fb⁻¹ and that achievable with 50 fb⁻¹ by the upgraded experiment assuming $\sqrt{s} = 14$ TeV. Note that at the upgraded LHCb, the yield per fb⁻¹, especially in hadronic B and D decays, will be higher on account of the software trigger. (Adapted from Ref. [70].)

⁷¹⁷ investigated. The CMS (5.2 fb⁻¹ [78]) and ATLAS (4.9 fb⁻¹ [79]) Collaborations have also performed such ⁷¹⁸ studies. The results agree with the SM and the previous measurements, but have larger errors than LHCb.

⁷¹⁹ Many other decays are being studied, including all-hadronic decays such as $B_s \to \phi \phi$ [80] (β_s^{eff} via interference

of mixing and decay via gluonic penguin) $B \to D\pi$, $B \to DK$ (determination of γ from tree processes), and

states with photons such as $B_s \to \phi \gamma$ (search for right-handed currents). The expected sensitivity to selected

⁷²² important *B* decays during present and upgraded phase of LHCb experiment is shown in Table 1-4.

The physics output of LHCb also extends beyond its *B* and charm (see next section) core programs. Examples of other topics include measurements of the production of electroweak gauge bosons in the forward kinematic region covered by the LHCb acceptance [81], studies of double parton scattering [82], measurements of the properties of exotic hadrons [83, 84], searches for lepton number and lepton flavor violations [85, 86] and for

⁷²⁷ long-lived new particles [87].

728 ATLAS and CMS

Two detectors, CMS and ATLAS at the LHC, are designed to explore high mass and high- p_T phenomena to 729 look for new physics at the LHC. They must operate at luminosities of up to $10^{34} \,\mathrm{cm}^{-2} \mathrm{s}^{-1}$, which implies 730 the need to handle an average event pileup of ~ 20 . Both experiments can implement muon triggers with 731 relatively low thresholds of a few GeV/c. However, the rate of low- p_T muons from B decays competes for 732 scarce resources with the many other trigger signatures that could contain direct evidence of new physics. 733 Thus in practice, only B final states containing dimuons are well preserved through the trigger pipelines. The 734 trigger efficiency is lower than in LHCb but at higher luminosity. One example of this, discussed above, is the 735 rare decay $B_{d,s} \to \mu^+ \mu^-$. If ATLAS and CMS can maintain their trigger efficiency as the LHC luminosity 736 and energy increase, they can be competitive in this study. The decay $B^0 \to K^* \mu^+ \mu^-$ presents more 737 problems. The muons are softer and more difficult to trigger on and the limited $K-\pi$ separation increases 738

the background to the K^* . However, as illustrated by their preliminary results these two experiments can play a confirming role to LHCb in this study. Despite their limitations, these two experiments will collect large numbers of *B* decays and should be able to observe many new decay modes and new particles containing *b* and charmed quarks.

⁷⁴³ 1.5 Report of the Charm Task Force

744 1.5.1 Introduction to Charm Physics

Studies of charm quarks can be split into two broad categories. First, in indirect searches for New Physics affecting decays and oscillations, charm quarks furnish a unique probe of flavor physics in the up-quark sector, complimenting strange and bottom physics. Second, as a probe of Quantum Chromodynamics (QCD) charm aids our understanding of non-perturbative physics, since it is not much heavier than the characteristic scale $\Lambda \sim 1 \text{ GeV}$ of QCD. Overall, charm adds much to the core new physics thrusts in heavy flavor physics while also adding significant breadth to the program.

⁷⁵¹ Charm physics measurements allow for direct determination of the Cabibbo-Kobayashi-Maskawa (CKM) ⁷⁵² matrix elements $|V_{cs}|$ and $|V_{cd}|$, can also help improve the accuracy of $|V_{cb}|$ and $|V_{ub}|$ determined from B⁷⁵³ decays, and $|V_{ts}|$ and $|V_{td}|$ from B^0 and B_s^0 mixing. Part of this richness is due to the usefulness of charm ⁷⁵⁴ data in verifying lattice QCD (LQCD) results.

⁷⁵⁵ Indirect searches for New Physics with charm quarks provide competitive as well as complimentary con-⁷⁵⁶ straints to the results of direct searches at the Energy Frontier. One can classify searches in three broad ⁷⁵⁷ categories, according to their "Standard Model background".

⁷⁵⁸ 1. Searches in the processes that are allowed in the Standard Model.

- ⁷⁵⁹ New physics contributions may often be difficult to discern in this case, except in cases of sufficient ⁷⁶⁰ theoretical precision (e.g., leptonic decays of *D*-mesons, $D_q \rightarrow \ell \bar{\nu}$). Alternatively, testing relations that ⁷⁶¹ are only valid in the standard model, but not in BSM models, may prove advantageous; e.g., CKM ⁷⁶² triangle relations.
- ⁷⁶³ 2. Searches in the processes that are forbidden in the Standard Model at tree level.

Flavor-changing neutral current (FCNC) interactions occur in the Standard Model only through loops and are therefore suppressed. New Physics contributions can enter both at tree-level and from oneloop corrections. Examples include $D^0 - \overline{D}^0$ mixing, or inclusive and exclusive transitions mediated by $c \to u\gamma$ or $c \to u\ell\bar{\ell}$.

- Searches for CP violation in charm decays and oscillations should be included here as well, as they require at least two different pathways to reach the final state, at least one of which is FCNC transition.
- 3. Searches in the processes that are forbidden in the Standard Model.
- While these processes are generally very rare even in NP models, their observation, however, would
- constitute a high-impact discovery. Examples include searches for lepton- and baryon-number-violating
- transitions, such as $D^0 \to e^+ \mu^-$, $D^0 \to \bar{p}e^+$, etc.
- The QCD side of charm physics is also very vibrant. Recently, there has been much activity in "XYZ" state spectroscopy, in addition to continued studies of conventional charmonium. This provides a rich source of results in hadronic physics and radiative transitions.

1.5.2 Current and Future Experiments

Over the past decade, charm results have been dominated by results from detectors at the e^+e^- "flavor factories" BaBar, Belle, and CLEO-c. Currently, the BESIII experiment is running at charm threshold and Belle II, which will run at and near the $\Upsilon(4S)$, is under construction; both experiments have excellent capabilities in charm [88, 51]. While charm statistics are lower at threshold, the data is unique in its ability to measure strong phases and also excels at modes with neutrinos in the final state. The Belle II detector should begin physics running in 2016; charm from continuum fragmentation at *B*-factory energies is complimentary to threshold data.

At hadron machines, CDF was able to contribute due to displaced-vertex and muon triggers, producing notable results on $D^0 - \overline{D}^0$ oscillations. While muon triggers have produced some charm results from ATLAS and CMS, the current and future charm program at hadron colliders lies almost exclusively with the dedicated flavor experiment, LHCb. Many areas of charm physics are accessible at LHCb and the 2018 upgrade will enhance opportunities even more. Their physics reach [70, 89] is an important addition to the e^+e^- program.

⁷⁹¹ The BESIII program should continue at least until the end of the decade, and Belle II and LHCb will carry

charm physics well into the 2020's. One major decision point is the future of threshold charm after BESIII.

⁷⁹³ Currently, the Cabibbo Lab near Rome is preparing a threshold tau-charm factory proposal. Interest has

⁷⁹⁴ also been expressed by BINP at Novosibirsk and institutions in Turkey.

⁷⁹⁵ Leptonic and Semileptonic Decays and CKM triangle relations

⁷⁹⁶ In leptonic and semileptonic decays, all of the uncertainties from strong-interaction effects may be conve-⁷⁹⁷ niently parameterized as decay constants and form factors, respectively. The remainder of the theory is ⁷⁹⁸ straightforward weak-interaction physics. Indeed, comparing decay constants and form factors to LQCD ⁷⁹⁹ predictions allows one to exclude large portions of parameter space for NP models with charged scalars.

Leptonic decay rates depend on the square of both decays constants and CKM matrix elements. If one uses LQCD as in input, then $|V_{cq}|$ may be extracted. If the CKM matrix elements are taken from elsewhere (possibly unitarity constraints), then we can test LQCD results. In fact, by taking ratios of leptonic and semileptonic decays, one can cancel $|V_{cq}|$ to obtain pure LQCD tests.

This Cabibbo-suppressed leptonic decay $D^+ \to \mu\nu$ is only measurable at threshold charm machines. Currently, it is essentially determined via one CLEO-c result [90], although BESIII has a preliminary result based on a dataset 3.5 times larger [91]. This result, $f_D = (203.91 \pm 5.72 \pm 1.91)$ MeV, based on 2.9 fb⁻¹, is still statistics-limited.

The Cabibbo-favored $D_s^+ \to \mu\nu$, $\tau\nu$ process is easier in two respects. Unlike the D^+ case, where $\tau\nu$ is a relatively small effect, here it offers additional channels that enhance the utility of a dataset. In addition, *B* factories possess enough tagging power in continuum charm production to make the best current single measurement. The one drawback is that D_s production rates are smaller than D^+ . Currently, the best measurement of f_{D_s} is a preliminary result from Belle [92].

⁸¹³ Successful LQCD calculations of $D_{(s)}$ decay constants will give confidence in their results for B decay ⁸¹⁴ constants. And while f_B can be obtained from $B \to \tau \nu$, there is no analogous direct way to determine f_{B_s} . ⁸¹⁵ By contrast, in charm, both strange and non-strange decay constants are directly accessible.

 $\mathbf{25}$

The key semileptonic modes are $D^0 \to K^- e^+ \nu$, $\pi^- e^+ \nu$. Additional statistical power may be obtained by including the isospin related D^+ decays, but both CKM matrix elements are accessible without the need for the more experimentally challenging D_s decays. The form factors, $f_K(q^2)$ and $f_{\pi}(q^2)$, are useful tests of LQCD. One depends on similar LQCD calculations to extract $|V_{ub}|$ from $B \to \pi \ell \nu$ decays.

For leptonic charm decays, $f_{D_{(s)}}$ parameterizes the chance that the heavy and light quarks "find each other" in order to annihilate. Due to helicity suppression the rate goes as m_{ℓ}^2 ; many NP models could have a different parametric dependence on m_{ℓ}^2 . Models include extended Higgs sectors, which include new charged scalar states, or models with broken left-right symmetry, which include massive vector W_R^{\pm} states. New Physics can be discussed in terms of generalized couplings [93].

One can also search for New Physics by testing relations that hold in the SM, but not necessarily in general. An example of such relation is a CKM "charm unitarity triangle" relation:

$$V_{ud}^* V_{cd} + V_{us}^* V_{cs} + V_{ub}^* V_{cb} = 0.$$
(1.6)

Processes that are used to extract CKM parameters in Eq. (1.6) can be affected by New Physics. This can 827 lead to disagreement between CKM elements extracted from different processes, or the triangle not closing. 828 Finally, since all CP-violating effects in the flavor sector of the SM are related to the single phase of the 829 CKM matrix, all of the CKM unitarity triangles, have the same area, A = J/2, where J is the Jarlskog 830 invariant. This fact could provide a non-trivial check of the Standard Model, given measurements of more 831 than one triangle with sufficient accuracy. Unfortunately, the "charm triangle" will be harder to work with 832 than the familiar B physics triangle since it is rather "squashed". In terms of the Wolfenstein parameter 833 $\lambda = 0.22$, the relation in Eq. (1.6) has one side $\mathcal{O}(\lambda^5)$ with the other two being $\mathcal{O}(\lambda)$. 834

D^0 Oscillations (including CP Violation)

The presence of $\Delta C = 2$ operators produce off-diagonal terms in the $D^0 - \overline{D}^0$ mass matrix, mixing the flavor eigenstates into the mass eigenstates

$$|D_{1,2}\rangle = p|D^0\rangle \pm q|\overline{D}^0\rangle.$$
(1.7)

Neglecting CP violation leads to $|p| = |q| = 1/\sqrt{2}$. The mass and width splittings between the mass eigenstates are

$$x = \frac{m_1 - m_2}{\Gamma_D}, \qquad y = \frac{\Gamma_1 - \Gamma_2}{2\Gamma_D}, \tag{1.8}$$

where Γ_D is the average width of the two mass eigenstates.

The oscillation parameters, x and y are both of order 1% in the D^0 system. These small values require the high-statistics of B factories and hadron machines. Observations thus far have relied on time-dependence of several hadronic decays $K\pi$, $K\pi\pi^-$, $K_S\pi\pi$, etc., as well as lifetime differences between CP-eigenstate decays $(KK, \pi\pi)$ and the average lifetime (see the review in [57]). LHCb has made the highest significance (9σ) observation of D^0 oscillations in a single experiment [94]. However, a non-zero value of x has not yet been established at 3σ . LHCb and Belle II will be able to pinpoint the value of x in the next several years.

⁸⁴⁷ Theoretical predictions for x and y in the SM are uncertain, although values about 1% had been expected [95].

⁸⁴⁸ The predictions need to be improved over next several years. Several groups are working to understand the

⁸⁴⁹ problem using technology of heavy quark expansion and other long-distance methods, including lattice QCD.

However, one can place an upper bound on the NP parameters by neglecting the SM contribution altogether and assuming that NP saturates the experimental result. One subtlety is that the SM and NP contributions

⁸⁵² can have either the same or opposite signs. While the sign of the SM contribution cannot be calculated

reliably due to hadronic uncertainties, x computed within a given NP model can be determined. This stems from the fact that NP contributions are generated by heavy degrees of freedom making the short-distance OPE reliable. This means that only the part of parameter space of NP models that generate x of the same sign as observed experimentally can be reliably constrained.

Any NP degree of freedom will generally be associated with a generic heavy mass scale M, at which the NP interaction is most naturally described. At the scale m_c , this description must be modified by the effects of QCD. In order to see how NP might affect the mixing amplitude, it is instructive to consider off-diagonal terms in the neutral D mass matrix,

$$\left(M - \frac{i}{2}\Gamma\right)_{12} = \frac{1}{2M_{\rm D}} \langle \overline{D}^0 | \mathcal{H}_w^{\Delta C = -2} | D^0 \rangle + \frac{1}{2M_{\rm D}} \sum_n \frac{\langle \overline{D}^0 | \mathcal{H}_w^{\Delta C = -1} | n \rangle \langle n | \mathcal{H}_w^{\Delta C = -1} | D^0 \rangle}{M_{\rm D} - E_n + i\epsilon} , \qquad (1.9)$$

where the first term contains $\mathcal{H}_w^{\Delta C=-2}$, which is an effective $|\Delta C| = 2$ Hamiltonian, represented by a set of operators that are local at the $\mu \simeq m_D$ scale. This first term only affects x, but not y.

As mentioned above, heavy BSM degrees of freedom cannot be produced in charm meson decays, but can nevertheless affect the effective $|\Delta C| = 2$ Hamiltonian by changing Wilson coefficients and introducing new operator structures. By integrating out those new degrees of freedom associated with a high scale M, we are left with an effective Hamiltonian written in the form of a series of operators of increasing dimension. It turns out that a model-independent study of NP $|\Delta C| = 2$ contributions is possible, as any NP model will only modify Wilson coefficients of those operators [96, 97],

$$\mathcal{H}_{NP}^{|\Delta C|=2} = \frac{1}{M^2} \left[\sum_{i=1}^{8} C_i(\mu) \ Q_i(\mu) \right], \qquad \begin{array}{l} Q_1 = \left(\overline{u}_L^{\alpha} \gamma_{\mu} c_L^{\alpha} \right) \left(\overline{u}_L^{\beta} \gamma^{\mu} c_L^{\beta} \right) , \qquad Q_5 = \left(\overline{u}_R^{\alpha} c_L^{\beta} \right) \left(\overline{u}_L^{\beta} c_R^{\alpha} \right) , \\ Q_2 = \left(\overline{u}_R^{\alpha} c_L^{\alpha} \right) \left(\overline{u}_R^{\beta} c_L^{\beta} \right) , \qquad Q_6 = \left(\overline{u}_R^{\alpha} \gamma_{\mu} c_R^{\alpha} \right) \left(\overline{u}_R^{\beta} \gamma^{\mu} c_R^{\beta} \right) , \\ Q_3 = \left(\overline{u}_R^{\alpha} c_L^{\beta} \right) \left(\overline{u}_R^{\beta} c_L^{\alpha} \right) , \qquad Q_7 = \left(\overline{u}_L^{\alpha} c_R^{\alpha} \right) \left(\overline{u}_L^{\beta} c_R^{\beta} \right) , \\ Q_4 = \left(\overline{u}_R^{\alpha} c_L^{\alpha} \right) \left(\overline{u}_L^{\beta} c_R^{\beta} \right) , \qquad Q_8 = \left(\overline{u}_L^{\alpha} c_R^{\beta} \right) \left(\overline{u}_L^{\beta} c_R^{\beta} \right) , \end{array}$$

$$(1.10)$$

where C_i are dimensionless Wilson coefficients, and the Q_i are the effective operators; α and β are color indices. In total, there are eight possible operator structures contributing to $|\Delta C| = 2$ transitions. Taking operator mixing into account, a set of constraints on the Wilson coefficients of Eq. (1.10) can be placed,

$$(|C_1|, |C_2|, |C_3|, |C_4|, |C_5|) \le (57, 16, 58, 5.6, 16) \times 10^{-8} \left(\frac{M}{1 \text{ TeV}}\right)^2.$$
 (1.11)

The constraints on $C_6 - C_8$ are identical to those on $C_1 - C_3$ [97]. Note that Eq. (1.11) implies that New Physics particles have highly suppressed couplings to charm quarks. Alternatively, the tight constraints of Eq. (1.11) probe NP at the very high scales: $M \ge (4 - 10) \times 10^3$ TeV for tree-level NP-mediated charm mixing and $M \ge (1 - 3) \times 10^2$ TeV for loop-dominated mixing via New Physics particles.

There is a beautiful effect at threshold, where DCSD background cancels due to the quantum mechanics of 876 correlated $D^0 - \overline{D}^0$ pairs at the $\psi(3770)$, and like-sign $K^{\pm}\pi^{\mp}$ decays are purely due to mixing. However, this 877 requires high-quality particle ID, and is also very luminosity-intensive. The event rate is of order one event 878 per 5 fb^{-1} (the current BESIII dataset is 2.9 fb^{-1}). Threshold does come into play n a different manner, 879 however. When mixing is measured via the time dependence of hadronic decays, one measures x, y in a 880 rotated basis. These parameters, denoted x', y' in the case of $K \pm \pi^{\mp}$, can only be converted to the desired 881 x, y with knowledge of a strong final-state scattering phase, $\delta_{K\pi}$. Threshold charm data provide the only 882 possibility to measure this (and other related) phases. 883

Observable	Current Expt.	LHCb	Belle II	LHCb Upgrade
Observable		(5 fb^{-1})	(50 ab^{-1})	$(50 \ {\rm fb}^{-1})$
x	$(0.63 \pm 0.20)\%$	$\pm 0.06\%$	$\pm 0.02\%$	$\pm 0.02\%$
y	$(0.75 \pm 0.12)\%$	$\pm 0.03\%$	$\pm 0.01\%$	$\pm 0.01\%$
$y_{ m CP}$	$(1.11 \pm 0.22)\%$	$\pm 0.02\%$	$\pm 0.03\%$	$\pm 0.01\%$
q/p	0.91 ± 0.17	± 0.085	± 0.03	± 0.03
$\arg(q/p)$	$(-10.2 \pm 9.2)^{\circ}$	$\pm 4.4^{\circ}$	±1.4°	$\pm 2.0^{\circ}$

Table 1-5. Sensitivities of Belle II and LHCb to charm mixing related parameters, along with the current results for these measurements (here $\arg(q/p)$ means $\arg \lambda_{K^+K^-}$). The second column gives the 2011 world averages. The remaining columns give the expected accuracy at the indicated integrated luminosities. In the convention used in HFAG fits, in the absence of CP violation |q/p| = 1 and $\arg(q/p) = 0$.

CP violation in D oscillations is an important area for future work. In Table 1-5, we summarize the 884 prospects for future results on these topics. In particular, see the entries related to p, q, which are express 885 the D eigenstates in the D^0 , \overline{D}^0 basis. In the absence of CP violation |q/p| = 1 and $\arg q/p = 0$. 886

CP Violation in Decays 887

A possible manifestation of new physics interactions in the charm system is associated with the observation 888 of CP-violation [98, 99]. This is due to the fact that all quarks that build up the hadronic states in weak 889 decays of charm mesons belong to the first two generations. Since the 2×2 Cabibbo quark mixing matrix 890 is real, no CP violation is possible in the dominant tree-level diagrams which describe the decay amplitudes. 891 CP-violating amplitudes can be introduced in the Standard Model by including penguin or box operators 892 induced by virtual b quarks. However, their contributions are strongly suppressed by the small combination 893 of CKM matrix elements $V_{cb}V_{ub}^*$. Thus, it was believed that the observation of large CP violation in charm 894 decays or mixing would be an unambiguous sign for New Physics. The SM "background" here is quite small, 895 giving CP-violating asymmetries of the order of 10^{-3} . Thus, observation of CP-violating asymmetries larger 896 than 1% could indicate presence of new physics. 897

Recent measurements have indicated the possibility of direct CP violation in the decays $D^0 \to K^+ K^-$ 898 $D^0 \to \pi^+\pi^-$ [100]. The most recent LHCb result indicate that the difference of CP-violating asymmetries is 890

$$\Delta A_{\rm CP} = A_{\rm CP} (K^- K^+) - A_{\rm CP} (\pi^- \pi^+) = (0.49 \pm 0.30 \pm 0.14)\%.$$
(1.12)

The result of Eq. (1.12), as well as earlier data from LHCb and other experiments resulted in intense 900 theoretical discussion of a possible size of this quantity in the standard model and in some models of new 901 physics [101]. New measurements of individual direct CP-violating asymmetries entering Eq. (1.12), other 902 asymmetries in the decays of neutral and charged D's into PP, PV, and VV final states are needed to guide 903 theoretical calculations (of penguin amplitudes). 904

It is also important to measure CP-violating asymmetries in the decays of charmed baryon states, as those 905 could have different theoretical and experimental systematics and could provide better handle on theoretical 906 uncertainties. 907

No indirect CP violation has been observed in charm transitions yet. However, available experimental 908 constraints can provide some tests of CP-violating NP models. For example, a set of constraints on the 909

⁹¹⁰ imaginary parts of Wilson coefficients of Eq. (1.10) can be placed,

$$(\text{Im}C_1, \text{Im}C_2, \text{Im}C_3, \text{Im}C_4, \text{Im}C_5) \leq (11, 2.9, 11, 1.1, 3.0) \times 10^{-8} \left(\frac{M}{1 \text{ TeV}}\right)^2.$$
 (1.13)

Just like the constraints of Eq. (1.11), they give a sense of how NP particles couple to the Standard Model.

912 Rare Decays

⁹¹³ The flavor-changing neutral current (FCNC) decay $D^0 \to \mu^+ \mu^-$ is of renewed interest after the successful ⁹¹⁴ observation of $B_s \to \mu^+ \mu^-$. While heavily GIM-suppressed, long-distance contributions, from $D^0 \to \gamma \gamma$ for ⁹¹⁵ example, also contribute. Direct knowledge of the decay $D^0 \to \gamma \gamma$ allows one to limit these contributions to ⁹¹⁶ the di-muon mode to $< 6 \times 10^{-11}$.

⁹¹⁷ Decays $B \to K^{(*)}\ell^+\ell^-$ have been the subject of great interest for many years, both rates and angular ⁹¹⁸ distributions offer the chance to see new physics effects. The analogous charm decays, $D^+_{(s)} \to h^+\mu^+\mu^-$, ⁹¹⁹ $D^0 \to hh'\mu^+\mu^-$ are likewise interesting. The former modes have long-distance contributions of order 10^{-6} ⁹²⁰ from vector intermediaries (ρ, ω, ϕ) but these can be cut away. The Standard Model rate for the remaining ⁹²¹ decays is around 10^{-11} . For the latter modes, one can form forward-backward and *T*-odd asymmetries with ⁹²² sensitivity to new physics.

⁹²³ Experimentally, at present, there are only the upper limits on $D^0 \to \ell^+ \ell^-$ decays,

$$\mathcal{B}(D^0 \to \mu^+ \mu^-) \le 1.1 \times 10^{-8}, \qquad \mathcal{B}(D^0 \to e^+ e^-) \le 7.9 \times 10^{-8}, \qquad \mathcal{B}(D^0 \to \mu^\pm e^\mp) \le 2.6 \times 10^{-7}.$$
(1.14)

Theoretically, just like in the case of mixing discussed above, all possible NP contributions to $c \rightarrow u\ell^+\ell^$ can also be summarized in an effective Hamiltonian,

$$\begin{aligned}
\widetilde{Q}_{1} &= (\overline{\ell}_{L} \gamma_{\mu} \ell_{L}) (\overline{u}_{L} \gamma^{\mu} c_{L}) , \qquad \widetilde{Q}_{4} = (\overline{\ell}_{R} \ell_{L}) (\overline{u}_{R} c_{L}) , \\
\widetilde{Q}_{2} &= (\overline{\ell}_{L} \gamma_{\mu} \ell_{L}) (\overline{u}_{R} \gamma^{\mu} c_{R}) , \qquad \widetilde{Q}_{5} = (\overline{\ell}_{R} \sigma_{\mu\nu} \ell_{L}) (\overline{u}_{R} \sigma^{\mu\nu} c_{L}) , \\
\widetilde{Q}_{3} &= (\overline{\ell}_{L} \ell_{R}) (\overline{u}_{R} c_{L}) ,
\end{aligned}$$
(1.15)

where \tilde{C}_i are again Wilson coefficients, and the \tilde{Q}_i are the effective operators. In this case, however, there are ten of them, with five additional operators $\tilde{Q}_6, \ldots, \tilde{Q}_{10}$ that can be obtained from operators in Eq. (1.15) by the substitutions $L \to R$ and $R \to L$. Further details may be found in Ref. [102], where it is also noted that it might be advantageous to study correlations of New Physics contributions to various processes, for instance $D^0 - \overline{D}^0$ mixing and rare decays.

931 Strong Phases

Threshold data with correlated $D^0 - \overline{D}^0$ pairs may be used to extract strong phases in D decays. These phases enter into B physics determinations of the CKM angle γ from $B \to D^{(*)}K^{(*)}$ decays [103]. Without direct input from charm, these B results suffer from ill-defined systematic uncertainties and lose precision.

In addition, related strong phases are needed to related observables of $D^0 - \overline{D}^0$ oscillations measured with

hadronic final states to the usual x, y parameters.

937 Charmonium and Spectroscopy

Recent observation of conventional charmonium states [104] such as the h_c and $\eta_c(2S)$ are accompanied by continuing discoveries of more "XYZ" exotic states [105].

The spectroscopy of conventional states can be used to calibrate LQCD, and many γ (both E1 and M1), $\pi^0, \eta, \pi\pi$ transitions have been studied. The *XYZ* states are a challenge to QCD, and may include tetraquarks, $c\bar{c}g$ hybrids, meson molecules, etc. Experimental data continues to accumulate, giving more input to a vibrant field, testing many theoretical ideas.

944 Other Topics

We finally list a few topics on "engineering numbers". Currently, charm lifetimes are dominated by FOCUS results; while the results are well-respected, a cross-check would be welcome. These results sever to relate theoretical predictions for partial widths to the experimentally accessible quantities, branching fractions.

Likewise, golden mode branching fractions for D mesons are dominated by CLEO-c; a cross-check from BESIII is in order. For the baryons, where there are four weakly-decaying ground states, there are no absolute branching fraction results. For $\Lambda_c \to pK^-\pi^+$, the near-threshold enhancement of Λ_c pairs measured by Belle in ISR [106] shows that BESIII should be able to provide a nice result with a modest-length run.

In addition to topics discussed above, charm quarks will play a major role in the heavy-ion experimental programs at RHIC and LHC for the next decade. Questions that will be addressed include identification of the exact energy loss and hadronization mechanisms of charm (or beauty) quarks in propagation through

⁹⁵⁵ Quark-Gluon Plasma (QGP), calculations of heavy quark transport coefficients, etc.

⁹⁵⁶ 1.5.3 Charm Physics Summary and Perspectives Beyond 2020

⁹⁵⁷ Continued support of BESIII, LHCb, and Belle II is critical to U.S. involvement in a vibrant charm program.
 ⁹⁵⁸ Investments in the first two are rather modest, yet provide valuable access to exciting datasets. Attention
 ⁹⁵⁹ should also be payed to possible opportunities at a future threshold experiment should one be built abroad.

Theoretical calculations in charm physics are mainly driven by experimental results. The challenges asso-960 ciated with non-perturbative QCD dynamics are being addressed by advances in lattice QCD and other 961 non-perturbative approaches. While similar probes of the NP scale that might reveal the "grand design" 962 of flavor are available in the strange and beauty systems, charm quarks furnish unique access to processes 963 involving up quarks, at least until equally precise data becomes available in the decays of top quarks, where 964 non-perturbative QCD effects are less important. Yet, even in this case neutral mesons containing charm 965 quark are the only mesons in that sector that can have flavor oscillations and thus probe NP in the $\Delta F = 2$ 966 transitions. 967

⁹⁶⁸ 1.6 Report of the Lattice QCD Task Force

The properties of the five least massive quarks offer a powerful tool to indirectly study physics at energies many orders of magnitude above those which are accessible to present or planned accelerators. This is

⁹⁷¹ made possible in large part by the quarks' strong interactions which provide experimental physics with a

Quantity	CKM	Present	2007 forecast	Present	2018
	element	expt. error	lattice error	lattice error	lattice error
f_K/f_{π}	$ V_{us} $	0.2%	0.5%	0.4%	0.15%
$f_+^{K\pi}(0)$	$ V_{us} $	0.2%	—	0.4%	0.2%
f_D	$ V_{cd} $	4.3%	5%	2%	< 1%
f_{D_s}	$ V_{cs} $	2.1%	5%	2%	< 1%
$D \to \pi \ell \nu$	$ V_{cd} $	2.6%	_	4.4%	2%
$D\to K\ell\nu$	$ V_{cs} $	1.1%	_	2.5%	1%
$B\to D^*\ell\nu$	$ V_{cb} $	1.3%	_	1.8%	< 1%
$B \to \pi \ell \nu$	$ V_{ub} $	4.1%	_	8.7%	2%
f_B	$ V_{ub} $	9%	_	2.5%	< 1%
ξ	$\left V_{ts}/V_{td}\right $	0.4%	2-4%	4%	< 1%
Δm_s	$ V_{ts}V_{tb} ^2$	0.24%	$7 ext{-}12\%$	11%	5%
B_K	${\rm Im}(V_{td}^2)$	0.5%	3.5– $6%$	1.3%	< 1%

Table 1-6. History, status and future of selected lattice-QCD calculations needed for the determination of CKM matrix elements. 2007 forecasts are from Ref. [108]. Most present lattice results are taken from latticeaverages.org [109]. The quantity ξ is $f_{B_s} \sqrt{B_{B_s}}/(f_B \sqrt{B_B})$.

host of bound states, common and rare decay processes and mixings that enable clever and highly sensitive studies of the properties of the underlying quarks. Until recently, the lack of predictive control of these same strong interactions provided a large barrier to fully exploiting this potential. *Ab initio* lattice calculations are systematically removing this barrier, allowing us to fully exploit the strong interactions of the quarks to search for physics beyond the Standard Model. In this section we describe the status and prospects for the lattice QCD calculations needed for future quark-flavor experiments. Much of this material is drawn from a recent USQCD (the national US lattice-QCD collaboration) white paper [107].

⁹⁷⁹ Lattice QCD provides a first-principles method for calculating low-energy hadronic matrix elements with
 reliable and systematically-improvable uncertainties. Such matrix elements — decays constants, form factors,
 mixing matrix elements, etc. — are needed to determine the Standard Model (SM) predictions for many
 processes and/or to extract CKM matrix elements.

In the last five years lattice QCD has matured into a precision tool. Results with fully controlled errors are available for nearly 20 matrix elements: the decay constants f_{π} , f_K , f_D , f_{D_s} , f_B and f_{B_s} , semileptonic form factors for $K \to \pi$, $D \to K$, $D \to \pi$, $B \to D$, $B \to D^*$, $B_s \to D_s$ and $B \to \pi$, and the four-fermion mixing matrix elements B_K , $f_B^2 B_B$ and $f_{B_s}^2 B_{B_s}$. By contrast, in 2007 (when the previous USQCD white paper was written [108]), only f_K/f_{π} was fully controlled. A sample of present errors is collected in Table 1-6. For Kmesons, errors are at or below the percent level, while for D and B mesons errors range from few to ~10%.

The lattice community is embarking on a three-pronged program of future calculations: (i) steady but significant improvements in "standard" matrix elements of the type just described, leading to much improved results for CKM parameters (e.g., V_{cb}); (ii) results for many additional matrix elements relevant for searches for new physics and (iii) the extension of lattice methods to more challenging matrix elements which can both make use of old results and provide important information for upcoming experiments.

31

Reducing errors in the standard matrix elements has been a major focus of the lattice community over the last 994 five years, and the improved results illustrated in Table 1-6 now play an important role in the determination 995 of the CKM parameters in the "unitarity triangle fit." Lattice-QCD calculations involve various sources 996 of systematic error (the need for extrapolations to zero lattice spacing, infinite volume and the physical 997 light-quark masses, as well as fitting and operator normalization) and thus it is important to cross-check 998 results using multiple discretizations of the continuum QCD action. (It is also important to check that 999 results for the hadron spectrum agree with experiment. Examples of these checks are shown in the 2013 1000 whitepaper [107].) This has been done for almost all the quantities noted above. This situation has spawned 1001 two lattice averaging efforts, latticeaverages.org [109] and FLAG-1 [110], which have recently joined 1002 forces and expanded to form a worldwide Flavor Lattice Averaging Group (FLAG-2), with first publication 1003 expected in mid-2013. 100

The ultimate aim of lattice-QCD calculations is to reduce errors in hadronic quantities to the level at which 1005 they become subdominant either to experimental errors or other sources of error. As can be seen from 1006 Table 1-6, several kaon matrix elements are approaching this level, while lattice errors remain dominant 1007 in most quantities involving heavy quarks. Thus the most straightforward contribution of lattice QCD to 1008 the future intensity frontier program will be the reduction in errors for such quantities. Forecasts for the 1009 expected reductions by 2018 are shown in the table. These are based on a Moore's law increase in computing 1010 power, and extrapolations using existing algorithms. Past forecasts have been typically conservative (as 1011 shown in the table) due to unanticipated algorithmic or other improvements. The major reasons for the 1012 expected reduction in errors are the use of u and d quarks with physical masses, the use of smaller lattice 1013 spacings and improved heavy-quark actions, and the reduction in statistical errors. 1014

Thus one key contribution of lattice QCD to the future flavor-physics program will be a significant reduction in the errors in CKM elements, most notably V_{cb} . This feeds into the SM predictions for several of the rare decays that are part of the proposed experimental program, e.g., $K \to \pi \nu \bar{\nu}$. For these decays, the parametric error from $|V_{cb}|$, which enters as the fourth power, is the dominant source of uncertainty in the SM predictions. The lattice-QCD improvements projected in Table 1-6 will bring the theoretical uncertainties to a level commensurate with the projected experimental errors in time for the planned rare kaon-decay experiments at Fermilab.

The matrix elements discussed so far involve only a single hadron and no quark-disconnected contractions. 1022 These are the most straightforward to calculate (and are sometimes called "gold-plated"). The second part 1023 of the future lattice-QCD program for the intensity frontier will be the extension of the calculations to 1024 other, similar, matrix elements which are needed for the search for new physics. This includes the mixing 1025 matrix elements for kaons, D and B mesons arising from operators present in BSM theories but absent in 1026 the SM, the form factors arising in $B \to K\ell^+\ell^-$ and $\Lambda_b \to \Lambda\ell^+\ell^-$, non-SM form factors for $K \to \pi, B \to \pi$ 1027 and $B \to K$ transitions. We expect the precision attained for these quantities to be similar to those for 1028 comparable quantities listed in Table 1-6. 1029

The third part of the lattice-QCD program is the least developed and most exciting. This involves the 1030 development of new methods or the deployment of known but challenging methods, and allows a substantial 1031 increase in the repertoire of lattice calculations. In particular, calculations involving two particles below 1032 the inelastic threshold are now possible (e.g., $K \to \pi\pi$ amplitudes [111, 112, 113]), quark-disconnected 1033 contractions are being controlled (e.g., η' and η masses [114] and the nucleon sigma term [115]) and 1034 processes involving two insertions of electroweak operators are under pilot study (e.g., the long-distance 1035 part of Δm_K [116]). During the next five years, we expect that these advances will lead to a quantitative 1036 understanding of the $\Delta I = 1/2$ rule, a prediction with ~ 5% errors for the the SM contribution to ϵ' , and 1037 predictions with 10–20% errors for the long-distance contributions to Δm_K and ϵ_K . This will finally allow 1038 us to use these hallowed experimental results in order to search for new physics. 1039

These new methods should allow lattice QCD to contribute directly to the proposed flavor-physics experiments. For example, a calculation of the long-distance contributions to $K \to \pi \nu \bar{\nu}$ decays should be possible, checking the present estimate that these contributions are small. Similar methods should allow the calculation of the sign of the CP-conserving amplitude $K_L \to \pi^0 e^- e^+$, thus resolving a major ambiguity in the SM prediction for $K_S \to \pi^0 e^- e^+$.

We also expect progress on even more challenging calculations, for which no method is yet known. An important example, in light of recent evidence for CP-violation in D decays and for $D - \overline{D}$ mixing, is to develop a method for calculating the amplitudes for $D \to \pi\pi$, KK decays and $D - \overline{D}$ mixing. This requires dealing with four or more particles in a finite box, as well as other technical details.

These plans rely crucially on access to high-performance computing, as well as support for algorithm and software development. In the US, much of this infrastructure is coordinated by the USQCD umbrella collaboration. Continued support for this effort is essential for the program discussed here.

We also stress that there are substantial lattice-QCD efforts underway to calculate the hadronic (vacuum polarization and light-by-light) contributions to muonic g-2, the light- and strange-quark contents of the nucleon (which are needed to interpret $\mu \rightarrow e$ conversion and dark-matter experiments), and the nucleon axial form factor (which enters the determination of the neutrino flux at many accelerator-based neutrino experiments). Smaller-scale lattice-QCD calculations of nucleon EDMs, proton- and neutron-decay matrix elements, and neutron-antineutron oscillation matrix elements are also in progress. These are very important for the intensity frontier as a whole, although not directly relevant to quark-flavor physics.

In the remainder of this subsection, we describe the major new efforts that are underway or envisaged for the next 5 or so years, considering in turn kaons, D mesons and B mesons, and close with a 15 year vision.

1061 1.6.1 Future lattice calculations of kaon properties

 $\frac{K \to \pi \pi \text{ amplitudes:}}{\text{state pions can be arranged to have physical, energy-conserving relative momentum by imposing appropriate$ boundary Corrections for the effects of working in finite volume can be made following the analysis ofRef. [117]. A first calculation of the amplitude to the <math>I = 2 two-pion state, A_2 , has been performed [111] with physical kinematics but 15% finite lattice spacing errors. Calculations are now underway using two ensembles with smaller lattice spacings which will allow a continuum extrapolation, removing this error. Results with an overall systematic error of $\approx 5\%$ are expected within the coming year.

The calculation of A_0 is much more difficult because of the overlap between the $I = 0 \pi \pi$ state and the 1069 vacuum, resulting in disconnected diagrams and a noise to signal ratio that grows exponentially with time 1070 separation. In addition, for I = 0, G-parity boundary condition must be employed and imposed on both 1071 the valence and sea quarks. These topics have been actively studied for past three years [118] and G-parity 1072 boundary conditions successfully implemented [119]. First results with physical kinematics are expected 1073 within two years from a relatively coarse, $32^3 \times 64$ ensemble. Errors on ϵ' on the order of 15% should be 1074 achieved, with the dominant error coming from the finite lattice spacing. As in the case of the easier A_2 1075 calculation, lessons learned from this first, physical calculation will then be applied to calculations using a 1076 pair of ensembles with two lattice spacings so that a continuum limit can be obtained. A five-year time-frame 1077 may be realistic for this second phase of the calculation. Essential to the calculation of both A_0 and A_2 is the 1078 renormalization of the lattice operators. Significant efforts will be required in the next 2-3 years to extend 1079 the range of non-perturbative renormalization methods up through the charm threshold and to a scale of 1080 4–5 GeV where perturbative matching to the conventional MS scheme will have small and controlled errors. 108

Long-distance contributions to Δm_K and ϵ_K : Promising techniques have been developed which allow 1082 the calculation of the long-distance contribution to kaon mixing by lattice methods. By evaluating a four-1083 point function including operators which create and destroy the initial and final kaons and two effective weak 1084 four-quark operators, the required second order amplitude can be explicitly evaluated. Integrating the space-1085 time positions of the two weak operators over a region of fixed time extent T and extracting the coefficient 1086 of the term which grows linearly with T gives precisely both Δm_K and ϵ_K . This Euclidean space treatment 1087 of such a second-order process contains unphysical contributions which grow exponentially with T and must 108 be subtracted. The statistical noise remaining after this subtraction gives even the connected diagrams 1089 the large-noise problems typical of disconnected diagrams. Preliminary results suggest that this problem 1090 can be solved by variance reduction methods and large statistics [116]. Given the central importance of 1091 GIM cancellation in neutral kaon mixing, a lattice calculation that is not burdened by multiple subtractions 1092 must include the charm quark mass with consequent demands that the lattice spacing be small compared to 1093 $1/m_c$ — a substantial challenge for a calculation which should also contain physical pions in an appropriately 1094 large volume. Perturbative results [120] as well as the first lattice calculation [116] suggest that perturbation 1095 theory works poorly at energies as low as the charm mass, making the incorporation of charm in a lattice 1096 calculation a high priority. Given the challenge of including both physical pions and active charm quarks, 1097 the first calculation of Δm_K may take 4–5 years. Results for the long-distance part of ϵ_K may be obtained 1098 in a similar time frame. However, a more challenging subtraction procedure must be employed for ϵ_K . 1099

Rare kaon decays: Given the promise of the first calculations of the long distance contributions to Δm_K , a process that involves two W^{\pm} exchanges, it is natural to consider similar calculations for the secondorder processes which enter important rare kaon decays such as $K_L^0 \to \pi^0 \ell^+ \ell^-$ and $K^+ \to \pi^+ \nu \bar{\nu}$. While in principle $K_L \to \ell^+ \ell^-$ should also be accessible to lattice methods, the appearance of three electroweak, hadronic vertices suggests that this and similar processes involving $H_W^{\Delta S=1}$ and two photons, should be tackled only after success has been achieved with more accessible, second order processes.

The processes $K^+ \to \pi^+ \nu \overline{\nu}$ and $K_L \to \pi^0 \nu \overline{\nu}$ may be the most straightforward generalization of the current 1106 Δm_K calculation. Here the dominant contribution comes from box and Z-penguin diagrams involving top 1107 quarks, but with a 30% component of the CP-conserving process coming from the charm quark [121]. While 1108 the charm quark piece is traditionally referred to as "short distance," the experience with Δm_K described 1109 above suggests that a non-perturbative evaluation of this charm-quark contribution may be a necessary check 1110 of the usual perturbative approach, which is here believed to be reliable. There are also "longer distance" 1111 contributions which are only accessible to lattice methods and will become important when the accuracy of 1112 rare kaon decay experiments reaches the 3% level, or possibly sooner. The long-distance contributions to 1113 the decay $K_{L/S} \to \pi^0 \ell^+ \ell^-$ also appear to be a natural target for a lattice-QCD calculation since the sign of 1114 the CP-conserving process $K_S \to \pi^0 \ell^+ \ell^-$ may be only determined this way. 1115

1116 1.6.2 Future lattice calculations of *D*-meson properties

¹¹¹⁷ $D \to \pi\pi$, *KK* amplitudes: Recent experimental evidence suggests that there may be CP-violation in ¹¹¹⁸ $D \to \pi\pi$ and $D \to KK$ decays. In order to interpret these results, it is essential to be able to predict the CP-¹¹¹⁹ violation expected in the SM. Even a result with a large, but reliable, error could have a large impact. This ¹¹²⁰ need will become even more acute over the next five years as LHCb and Belle II improve the measurements.

This calculation is more challenging than that for $K \to \pi\pi$ decays, which represent the present frontier of lattice calculations. In the kaon case, one must deal with the fact that two-pion states in finite volume are not asymptotic states, and the presence of multiple quark-disconnected contractions. For D decays, even when one has fixed the strong-interaction quantum numbers of a final state (say to I = S = 0), the strong

interactions necessarily bring in multiple final states: $\pi\pi$ and $K\bar{K}$ mix with $\eta\eta$, 4π , 6π , etc. The finite-1125 volume states used by lattice QCD are inevitably mixtures of all these possibilities, and one must learn how, 1126 in principle and in practice, to disentangle these states to obtain the desired matrix element. Recently, a 1127 first step towards developing a complete method has been taken [122], in which the problem has been solved 1128 in principle for any number of two-particle channels, and assuming that the scattering is dominantly S wave. 1129 This is encouraging, and this method may allow one to obtain semi-quantitative results for the amplitudes of 1130 interest. We expect that turning this method into practice will take ~ 5 years due to a number of numerical 1131 challenges (in particular the need to calculate several energy levels with good accuracy). 1132

In the more distant future, we expect that it will be possible to generalize the methodology to include four particle states; several groups are actively working on the theoretical issues and much progress has been made already for three particles.

¹¹³⁶ $D - \overline{D}$ mixing: Mixing occurs in the $D-\overline{D}$ system, although there is no clear evidence yet for CP violation ¹¹³⁷ in this mixing [57]. The short-distance contributions can be calculated for D mesons using lattice QCD, ¹¹³⁸ as for kaons and B mesons. The challenge, however, is to calculate the long-distance contributions. As in ¹¹³⁹ the case of Δm_K discussed above, there are two insertions of the weak Hamiltonian, with many allowed ¹¹⁴⁰ states propagating between them. The D system is much more challenging, however, since, as for the decay ¹¹⁴¹ amplitudes, there are many strong-interaction channels having $E < m_D$. Further theoretical work is needed ¹¹⁴² to develop a practical method.

1143 1.6.3 Future lattice calculations of *B*-meson properties

¹¹⁴⁴ $\underline{B} \rightarrow D^{(*)} \ell \nu$ form factors at nonzero recoil: Lattice-QCD results for these form factors allow for the ¹¹⁴⁵ determination of $|V_{cb}|$ from the measured decay rates. For the $B \rightarrow D^* \ell \nu$ form factor at zero recoil, the gap ¹¹⁴⁶ between experimental errors (1.3%) and lattice errors (presently ~ 1.8%) has narrowed considerably over ¹¹⁴⁷ the last five years. In the next five years, we expect the lattice contribution to the error in $|V_{cb}|$ to drop ¹¹⁴⁸ below the experimental one, as shown in Table 1-6. Particularly important for this will be the extension of ¹¹⁴⁹ the $B \rightarrow D^{(*)} \ell \nu$ form-factor calculations to nonzero recoil [123].

Tauonic B-decay matrix elements: Recently the BABAR collaboration measured the ratios $R(D^{(*)}) =$ 1150 $\mathcal{B}(B \to D^{(*)}\tau\nu)/\mathcal{B}(B \to D^{(*)}\ell\nu)$ with $\ell = e$ or μ , and observed a combined excess over the existing SM 1151 predictions of 3.4σ [124]. Those SM predictions were based, however, on models of QCD, not *ab initio* 1152 QCD. Realizing that it was much easier to obtain accurate results for these ratios than for the form-factors 1153 themselves, the Fermilab-MILC collaboration responded quickly (using lattice data already in hand), and 1154 provided the first lattice-QCD result for R(D) [125]. Their result slightly reduced the discrepancy with 1155 experiment for R(D) from $2.0 \rightarrow 1.7\sigma$. At present, the experimental errors in R(D) (~16%) dominate over 1156 lattice errors (4.3%), so further lattice improvements are not needed in the short run. The experimental 1157 uncertainties will shrink with the increased statistics available at Belle II, and it should be straightforward 1158 to reduce the corresponding lattice-QCD error by a factor of two over the next five years. Work is also in 1159 progress to calculate $R(D^*)$, for which the uncertainties are expected to be comparable to those of R(D). 1160

Belle II will also reduce the uncertainty in the experimental measurement of $\mathcal{B}(B \to \tau \nu)$ to the few-percent level with its anticipated full data set. In the next five years, lattice-QCD calculations are expected to reduce the error in f_B to the percent level (see Table 1-6). Particularly important for this will be the use of finer lattice spacings that permit relativistic *b*-quark actions [126]. Combined with the anticipated experimental precision, this will increase the reach of new-physics searches in $B \to \tau \nu$; moreover, correlations between $B \to \tau \nu$ and $B \to D^{(*)} \tau \nu$ decays can help distinguish between new-physics models. $\begin{array}{ll} B \rightarrow K\ell^{+}\ell^{-} \text{ and related decay form factors:} \\ \hline B \rightarrow K\ell^{+}\ell^{-} \text{ and related decay form factors:} \\ \hline B \rightarrow K\ell^{+}\ell^{-} \text{ and related decay form factors:} \\ \hline B \rightarrow K\ell^{+}\ell^{-} \text{ is now well measured, and increasingly accurate results from LHCb, and eventually Belle II, are expected. The SM prediction requires knowledge of the vector and tensor <math>b \rightarrow s$ form factors across the kinematic range. Present theoretical estimates use light-cone sum rules, but several first-principles lattice-QCD calculations are nearing completion, as reviewed in Ref. [127]. The calculation is similar to that needed for the $B \rightarrow \pi\ell\nu$ form factor, and we expect similar accuracy to be obtained over the next five years.

A related process is the baryonic decay $\Lambda_b \to \Lambda \ell^+ \ell^-$, recently measured by CDF. Here the extra spin degree of freedom can more easily distinguish between SM and BSM contributions. A lattice-QCD calculation of the required form factors has recently been completed, using HQET to describe the *b* quark [128]. Errors of ~ 10–15% in the form factors are obtained, which are comparable to present experimental errors. The latter errors will decrease with new results from LHCb, and so improved LQCD calculations and cross-checks are needed. Although the calculation is conceptually similar to that for $B \to K \ell^+ \ell^-$, given the presence of baryons we expect the errors for $\Lambda_b \to \Lambda \ell^+ \ell^-$ to lag somewhat behind.

Non-Standard Model form factors for $K \to \pi$ and $B \to \pi$ transitions: The $B \to K$ vector and 1180 tensor form factors just discussed are also needed to describe decays involving missing energy, $B \to KX$, in 1181 BSM theories [32]. Analogous form factors are needed for $B \to \pi X$ and $K \to \pi X$ decays. The tensor form 1182 factors are also needed to evaluate some BSM contributions to $K \to \pi \ell^+ \ell^-$ [129]. Thus it is of interest to 1183 extend the present calculations of vector form factors in $K \to \pi$ and $B \to \pi$ to include the tensor matrix 1184 elements. Since these are straightforward generalizations of present calculations, we expect that comparable 1185 accuracy to the present errors in Table 1-6 can be obtained quickly, and that future errors will continue to 1186 follow the projections for similar matrix elements. 1187

1188 1.6.4 Lattice QCD and flavor physics: 2018-2030

The discussion above has laid out an ambitious vision for future lattice-QCD calculations on a five-year 1189 timescale, explaining how they can provide essential and timely information for upcoming quark-flavor 1190 experiments. Also discussed are a number of more challenging quantities which have become accessible to 1191 lattice methods only recently. In this section we discuss more generally the opportunities offered by lattice 1192 methods over the extended time period covered by the Snowmass study. However, we should emphasize 1193 that these longer range forecasts are made difficult by the very rapid evolution of this emerging field, which 1194 is driven by both rapidly advancing commercial computer technology and continual, difficult-to-anticipate 1195 advances in algorithms. 1196

We begin with the conservative assumptions that exascale performance (10^{18} floating point operations/second) 1197 will be achieved by 2020, and that a further factor of 100 will be available by 2030. These represent factors 1198 of 10^2 and 10^4 over presently available capability. At fixed physical quark masses, the difficulty of modern 1199 lattice-QCD algorithms scales with decreasing lattice spacing a as $1/a^6$ and with increasing physical linear 1200 problem size L as L^5 . Present large-scale lattice calculations at physical quark masses are performed in 1201 volumes of linear size $L \approx 6$ fm and with inverse lattice spacing 1/a as small as ~ 2.5 GeV. Thus, these 10^2 1202 and 10^4 advances in computer capability will allow an increase in physical volume to 15 and 36 fm and in 1203 inverse lattice spacing to 5 and 10 GeV, respectively. Statistical errors can be reduced from their present 1204 percent-level for many quantities to 0.1% or even 0.01% as needed. 1205

These three directions of substantial increase in capability translate directly into physics opportunities. The large increase in possible Monte Carlo statistics is necessary if we are to decrease the errors on many of the quantities in Table 1-6 to the 0.1% level. Such increased statistics will also directly support perhaps 1% precision for results that depend on disconnected diagrams such as ϵ' and the $K_L - K_S$ mass difference. For most QCD calculations, the non-zero pion mass implies that finite volume effects decrease exponentially in the linear size of the system. However, this situation changes dramatically when electromagnetic effects are included. Here the massless photon and related difficulties of dealing with charged systems in finite volume result in substantial finite volume errors which decrease only as a power of L as the linear system size Lbecomes large. The ability to work on systems of linear size 20 or 30 fm will play an important role in both better understanding electromagnetic effects using lattice methods and achieving the 10% errors in the computation of such effects that are needed to attain 0.1% errors in many of the quantities in Table 1-6.

Finally the ability to work with an inverse lattice spacing as large as 10 GeV will allow substantial improve-1217 ments in the treatment of heavy quarks. Using 3 GeV $\leq 1/a \leq 5$ GeV, calculations involving charm quarks 1218 will have controlled finite lattice spacing errors on the 1% level or smaller. As a result calculation of the 1219 long-distance contributions, up to and including the charm scale, will be possible for Δm_K , ϵ_K and rare kaon 1220 decays yielding errors of order 1% for these important quantities. The larger inverse lattice spacings in the 1221 range 6 GeV $\leq 1/a \leq 10$ GeV will allow the present estimates of the finite lattice spacing errors in bottom 1222 quark systems to both be substantially reduced and to be refined using the new information provided by a 1223 larger range of lattice spacings. This will allow many quantities involving bottom quarks to be determined 1224 with errors well below 1%. 1225

While ever more difficult to forecast, a 10^4 increase in capability can be expected to significantly expand 1226 the range of quantities that can be computed using lattice methods. These include the $D - \overline{D}$ mixing and 1227 multi-particle D decays discussed in the previous section as well as even more challenging quantities such 1228 as semileptonic B decays with vector mesons in the final state. These are relevant both for the extraction 1229 of CKM matrix elements (e.g., $B \to \rho \ell \nu$ provides an alternative determination of $|V_{ub}|$) and new-physics 1230 searches (e.g., measurements of $B \to K^* \ell^+ \ell^-$, $B \to K^* \gamma$ and $B_s \to \phi \gamma$ probe $b \to s$ flavor-changing neutral 1231 currents). A second example is nonleptonic B decays, such as $B \to D\pi(K)$, which can be used to obtain the 1232 CKM angle γ . 1233

Clearly an enhanced computational capability of four orders of magnitude, coupled with possibly equally 1234 large advances in numerical algorithms, will have a dramatic effect on the phenomena that can be analyzed 1235 and precision that can be achieved using lattice methods. The possibility of making SM predictions with 1236 errors which are an order of magnitude smaller than present experimental errors will create an exciting 1237 challenge to identify quantities where substantially increased experimental accuracy is possible and where 1238 the impact of such measurements on the search for physics beyond the SM most sensitive. With the ability 1239 to make highly accurate SM predictions for a growing range of quantities, experiments can be designed 1240 that will achieve the greatest precision for quantities sensitive to physics beyond the SM, rather than being 1241 limited to those quantities which are least obscured by the effects of QCD. 1242

1243 1.7 A U.S. Plan for Quark Flavor Physics

Until recently, the U.S. had onshore accelerator facilities that supported a leadership role at both the Energy 1244 and Intensity Frontiers. With the successful start of the LHC and the termination of the Tevatron program, 1245 the Energy Frontier has migrated offshore for the foreseeable future. With choices summarized in Section 1.1. 1246 the U.S. has ceded leadership in much of quark-flavor physics. It is very difficult to foresee a scenario that 1247 leads to the construction of a facility in the U.S. that is capable of supporting B-physics or charm-physics 1248 experiments. Indeed, the only accelerator-based experiments currently in the DOE pipeline are neutrino 1249 experiments and muon experiments at Fermilab, and in the case of the neutrino program, the planning for 1250 the LBNE experiment was thrown into disarray with NSF's abandonment of the DUSEL initiative. Also, a 1251 central element needed for an LBNE experiment to achieve its potential, Fermilab's Project-X facility, has 1252 yet to achieve the first level of DOE approval ("mission need"). It is under these rather dire circumstances, 1253

facing the prospect that the U.S. accelerator-based HEP program may go the way of the dodo bird, that we must contemplate the question of whether and how the U.S. should pursue research in quark-flavor physics.

There is a strong physics case for quark-flavor physics that remains robust in all LHC scenarios. It rests, 1256 quite simply, on the potential of precision quark-flavor experiments and studies of very rare decays to obseve 1257 the effect of high-mass virtual particles. If new physics is observed at LHC, tighter constraints from the 1258 flavor sector will narrow the range of models that can account the observed states. If new physics is not 1259 discovered at LHC, then the reach to mass scales beyond that of LHC will still offer the potential to find new 1260 physics and to estimate the scale needed for direct observation. International recognition of the importance 1261 of quark-flavor physics is evident from the commitments in Europe and Asia to conduct the next-generation 1262 of B-physics, charm, and kaon experiments. 1263

In the U.S., predictably difficult budgets will impose limitations, but the goal should be to construct an HEP 1264 program that has the breadth to assure meaningful participation in making the discoveries that will define 1265 the future of this field. The successful U.S. contributions to LHC has demonstrated that physicists from 1266 U.S. laboratories and universities can play essential roles in offshore experiments. If this paradigm works at 1267 the Energy Frontier, it can work at the Intensity Frontier as well. Therefore, significant U.S. contributions 1268 to offshore quark-flavor experiments such as LHCb and Belle II should be encouraged. Also, in the one area 1269 where existing and foreseeable facilities on U.S. soil can support a world-leading program — kaon physics 1270 — the U.S. should embrace the opportunity. The accelerator facilities required for kaon experiments are 1271 exactly those needed for the neutrino program, so the costs are incremental and relatively modest. Below, 1272 we summarize the opportunities that exist now and those that will exist during the next decade. 1273

1274 1.7.1 Opportunities in This Decade

The Task Force reports have described current, planned, and possible B-physics, charm, and kaon experiments in Europe and Asia. There is a strong and diverse international program. The only U.S. entry in the discussion of the immediate future for quark-flavor physics experiments is the ORKA proposal at Fermilab, for an experiment which would make a precise measurement of the $K^+ \to \pi^+ \nu \bar{\nu}$ branching fraction.

For the remainder of this decade, the plans in Europe and Asia appear to be set, and the experiments there 1279 (those already running or under construction) will define the frontier of quark-flavor physics. These are 1280 LHCb and NA62 at CERN, KLOE2 in Italy, Panda in Germany, BESIII in China, and Belle II, KOTO, and 1281 TREK in Japan. This is a rich program, and fortunately U.S. physicists have some involvement in most 1282 of them. While all of these experiments have important physics goals and capabilities, the scale of LHCb 1283 and Belle II, and their incredibly broad physics menus including both bottom and charm, means that they 1284 will be the flagship experiments in quark-flavor physics. In view of that, the U.S. role in these experiments 1285 should be significant. 1286

The outstanding question is whether the ORKA experiment will go forward at Fermilab. It received "Stage 1" approval from the Fermilab in the fall of 2011, but has not been integrated into DOE or Fermilab planning thus far. A clear conclusion of this working group is that ORKA presents an extraordinary opportunity that should be pursued. Of course, with constrainted funding, this opportunity must be weighed against others outside the subject area of this working group. Nonetheless, if the U.S. HEP program endeavors to achieve a leading role at the Intensity Frontier, we believe that ORKA must be pursued.

¹²⁹³ In short, the optimal U.S. plan in quark-flavor physics for the remainder of this decade has four elements.

• U.S. physicists should be supported to carry out significant roles in LHCb and Belle II.

- The ORKA experiment should move forward in a timely way at Fermilab.
- Support for U.S participation on other experiments that are in progress (e.g., KOTO, TREK, BESIII) should be maintained.
- Support for theory, and the computing facilities needed for progress in Lattice QCD, should be maintained.

¹³⁰⁰ 1.7.2 Opportunities in the Next Decade

In the decade beginning around 2020, we can anticipate that LHCb will be well on its path toward collecting 50 fb⁻¹ and Belle II will be well on its path toward 50 ab⁻¹. These will be very complementary data samples, overlapping in some areas but providing different strengths in others. We cannot, of course, predict what the LHC experiments may have found by then, nor what surprising results may have come from any of the quark-flavor experiments discussed above. Based on what is learned between now and then, new priorities and new experimental directions may emerge.

Nonetheless, we anticipate that the U.S. HEP program will be continuing its emphasis on Intensity Frontier 1307 experiments, with a commitment to providing high-intensity proton sources for the production of neutrino 1308 beams for neutrino experiments. If so, then the potential for such a high-intensity proton source to support 1309 the next generation of rare kaon decay experiments is an opportunity unique to the U.S. program. In 1310 particular, Project-X at Fermilab can deliver more than an order of magnitude increase in the beam power 1311 available for producing kaons compared to any other laboratory in the world. In addition, the CW-linac 1312 of Project-X can provide a time structure that is programmable bunch-by-bunch. That capability can 1313 be exploited in neutral kaon experiments to measure the momentum of individual K_L^0 's via time-of-flight, 1314 opening the door to dramatic improvements in background rejection for some challenging rare decays. 1315

¹³¹⁶ Project-X can be the leading facility in the world for rare kaon decay experiments.

1317 **1.7.3** Conclusions

This report has described the physics case for precision studies of flavor-changing interactions of bottom, charm, and strange quarks, and it has described the experimental programs that are underway and foreseeable around the world. A substantial number of physicists in the U.S. are motivated to work in this area, both theorists and experimentalists. Quark-flavor physics should be a component in the plan for the future U.S. HEP program.

After enduring the full "Snowmass process", the Quark Flavor Physics working group has produced this report. It reflects a wide range of inputs. Its contents and conclusions have been publicly vetted. For instance, a draft of this report was posted for public comment.

¹³²⁶ Our major conclusions can be summarized as follows:

Quark flavor physics is an essential element in the international high-energy physics program. Experiments that study the properties of highly suppressed decays of strange, charm, and bottom quarks have the potential to observe signatures of new physics at mass scales well beyond those accessible by current or foreseeable accelerators.

- The importance of quark flavor physics is recognized in Europe and Asia, as demonstrated by the committments to LHCb, NA62, KLOE-2, and Panda in Europe, and to Belle-II, BES-III, KOTO, and TREK in Asia.
- In order for the U.S. HEP program to have the breath to assure meaningful participation in future discoveries, significant U.S. contributions to offshore quark-flavor experiments is important. In particular, U.S. contributions to LHCb and Belle II should be encouraged because of the richness of the physics menus of these experiments and their reach for new physics.
- Existing facilities at Fermilab are capable of mounting world-leading rare kaon decay experiments in this decade at modest incremental cost to running the Fermilab neutrino program. The proposed ORKA experiment, to measure the rare decay $K^+ \to \pi^+ \nu \overline{\nu}$ with high precision, provides such an opportunity. This is a compelling opportunity that should be exploited.
- Longer term, Project-X at Fermilab can become the dominant facility in the world for rare kaon decay experiments. Its potential to provide ultra-high intensity kaon beams with tunable time structure is unprecedented. The physics case for Project-X must be broader than its capabilities for kaon experiments, but the power of a Project-X kaon program is a strong argument in its behalf.
- Back-and-forth between theory and experiment is necessary for progress in quark-flavor physics, as in any field of physics. Therefore, stable support for theorists working in this area is essential. Lattice QCD also plays a critical role, and support for the computing facilities needed for LQCD progress should be maintained.

1350 References

- ¹³⁵¹ [1] J. L. Hewett *et al.*, arXiv:1205.2671 [hep-ex].
- ¹³⁵² [2] M. Kobayashi and T. Maskawa, Prog. Theor. Phys. 49, 652 (1973).
- ¹³⁵³ [3] N. Cabibbo, Phys. Rev. Lett. **10**, 531 (1963).
- ¹³⁵⁴ [4] S.L. Glashow, J. Iliopoulos, and L. Maiani, Phys. Rev. D 2, 1285 (1970).
- ¹³⁵⁵ [5] M.K. Gaillard and B.W. Lee, Phys. Rev. D **10**, 897 (1974).
- [6] A.I. Vainshtein and I.B. Khriplovich, Pisma Zh. Eksp. Theor. Fiz. 18, 141 (1973) [JETP Lett. 18, 83 (1973)].
- ¹³⁵⁸ [7] G. Isidori, Y. Nir and G. Perez, Ann. Rev. Nucl. Part. Sci. **60**, 355 (2010) [arXiv:1002.0900 [hep-ph]].
- [8] A. Höcker, H. Lacker, S. Laplace and F. Le Diberder, Eur. Phys. J. C 21 (2001) 225 [hep-ph/0104062];
 and updates at http://ckmfitter.in2p3.fr/.
- ¹³⁶¹ [9] J. Charles *et al.*, Eur. Phys. J. C **41** (2005) 1 [hep-ph/0406184].
- ¹³⁶² [10] L. Wolfenstein, Phys. Rev. Lett. **51**, 1945 (1983).
- ¹³⁶³ [11] A. Hocker and Z. Ligeti, Ann. Rev. Nucl. Part. Sci. 56 (2006) 501 [hep-ph/0605217].
- ¹³⁶⁴ [12] Z. Ligeti, Int. J. Mod. Phys. A **20**, 5105 (2005) [hep-ph/0408267].
- [13] M. Bona *et al.* [UTfit Collaboration], JHEP 0803, 049 (2008) [arXiv:0707.0636]; and updates at http:
 //utfit.org/.
- ¹³⁶⁷ [14] A. Lenz *et al.*, Phys. Rev. D **86** (2012) 033008 [arXiv:1203.0238 [hep-ph]].
- ¹³⁶⁸ [15] Y. Grossman, Z. Ligeti and Y. Nir, Prog. Theor. Phys. **122**, 125 (2009) [arXiv:0904.4262 [hep-ph]].
- ¹³⁶⁹ [16] J. Brod, contribution to "Kaon Physics with Project X", in Ref. [17].
- ¹³⁷⁰ [17] A. S. Kronfeld *et al.*, arXiv:1306.5009 [hep-ex].
- [18] S. Jäger, talk given at the NA62 Physics Handbook Workshop, http://indico.cern.ch/ get File.py/access?contribId=5&resId=0&materialId=slides&confId=65927
- [19] A. J. Buras, P. Gambino, M. Gorbahn, S. Jäger and L. Silvestrini, Nucl. Phys. B 592, 55 (2001)
 [hep-ph/0007313].
- ¹³⁷⁵ [20] M. Bauer, S. Casagrande, U. Haisch and M. Neubert, JHEP **1009**, 017 (2010) [arXiv:0912.1625 [hep-¹³⁷⁶ ph]].
- [21] M. Blanke, A. J. Buras, S. Recksiegel, C. Tarantino and S. Uhlig, JHEP 0706, 082 (2007)
 [arXiv:0704.3329 [hep-ph]].
- 1379 [22] A. J. Buras and L. Silvestrini, Nucl. Phys. B 546, 299 (1999) [hep-ph/9811471].
- [23] A. J. Buras, G. Colangelo, G. Isidori, A. Romanino and L. Silvestrini, Nucl. Phys. B 566, 3 (2000)
 [hep-ph/9908371].
- ¹³⁸² [24] U. Haisch, contribution to "Kaon Physics with Project X", in Ref. [17].
- ¹³⁸³ [25] S. Adler *et al.* (E949 & E787 Collaborations), Phys. Rev. **D77**:052003 (2008) [arXiv:0709.1000]
- ¹³⁸⁴ [26] Y. Grossman and Y. Nir, Phys. Lett. B **398**, 163 (1997) [hep-ph/9701313].
- ¹³⁸⁵ [27] M. Blanke, Acta Phys. Polon. **B41**:127 (2010), [arXiv:0904.2528]
- ¹³⁸⁶ [28] F. Mescia, C. Smith and S. Trine, JHEP **0608**, 088 (2006) [hep-ph/0606081].
- ¹³⁸⁷ [29] A. J. Buras, F. De Fazio and J. Girrbach, JHEP **1302**, 116 (2013) [arXiv:1211.1896 [hep-ph]].
- ¹³⁸⁸ [30] A. J. Buras, T. Ewerth, S. Jäger and J. Rosiek, Nucl. Phys. B **714**, 103 (2005) [hep-ph/0408142].

40

- [31] M. Blanke, A. J. Buras, B. Duling, K. Gemmler and S. Gori, JHEP 0903, 108 (2009) [arXiv:0812.3803
 [hep-ph]].
- ¹³⁹¹ [32] J. F. Kamenik and C. Smith, JHEP **1203**, 090 (2012) [arXiv:1111.6402 [hep-ph]].
- ¹³⁹² [33] V. Cirigliano and I. Rosell, Phys. Rev. Lett. **99**, 231801 (2007) [arXiv:0707.3439 [hep-ph]].
- [34] V. P. Efrosinin, I. B. Khriplovich, G. G. Kirilin and Y. .G. Kudenko, Phys. Lett. B 493, 293 (2000)
 (hep-ph/0008199).
- ¹³⁹⁵ [35] http://na62.web.cern.ch/na62/Documents/ReferenceDocuments.html.
- 1396 [36] http://koto.kek.jp/.
- 1397 [37] http://trek.kek.jp/.
- 1398 [38] http://www.lnf.infn.it/kloe2/.
- ¹³⁹⁹ [39] J. Comfort, et al., FERMILAB-PROPOSAL-1021 (2011).
- [40] KOPIO Experiment Proposal (2005), http://www.bnl.gov/rsvp/KOPIO.htm.
- [41] Lattice QCD at the intensity frontier, T. Blum et al. [USQCD Collaboration], available at http://www.
 usqcd.org/documents/13flavor.pdf.
- ¹⁴⁰³ [42] J. Zupan, arXiv:1101.0134 [hep-ph].
- ¹⁴⁰⁴ [43] R. Aaij *et al.* [LHCb Collaboration], arXiv:1304.2600 [hep-ex].
- ¹⁴⁰⁵ [44] R. Aaij et al. [LHCb Collaboration], Phys. Rev. Lett. **110** (2013) 021801 [arXiv:1211.2674 [hep-ex]].
- [45] A. J. Buras, J. Girrbach, D. Guadagnoli and G. Isidori, Eur. Phys. J. C 72 (2012) 2172 [arXiv:1208.0934
 [hep-ph]].
- ¹⁴⁰⁸ [46] V. M. Abazov *et al.* [D0 Collaboration], Phys. Rev. D **84** (2011) 052007 [arXiv:1106.6308 [hep-ex]].
- ¹⁴⁰⁹ [47] S. Laplace, Z. Ligeti, Y. Nir and G. Perez, Phys. Rev. D **65** (2002) 094040 [hep-ph/0202010].
- ¹⁴¹⁰ [48] Z. Xing [LHCb Collaboration], arXiv:1212.1175 [hep-ex].
- ¹⁴¹¹ [49] J. P. Lees et al. [BaBar Collaboration], arXiv:1303.0571 [hep-ex].
- ¹⁴¹² [50] S. Fajfer, J. F. Kamenik, I. Nisandzic and J. Zupan, Phys. Rev. Lett. **109**, 161801 (2012)
 ¹⁴¹³ [arXiv:1206.1872 [hep-ph]].
- ¹⁴¹⁴ [51] T. Aushev et al. [Belle II Collaboration], arXiv:1002.5012 [hep-ex].
- ¹⁴¹⁵ [52] M. Bona *et al.* [SuperB Collaboration], [arXiv:0709.0451 [hep-ex]].
- ¹⁴¹⁶ [53] I. Adachi et al. [Belle Collaboration], Phys. Rev. Lett. **108** (2012) 171802 [arXiv:1201.4643 [hep-ex]].
- ¹⁴¹⁷ [54] B. Aubert *et al.* [BaBar Collaboration], Phys. Rev. D **79** (2009) 072009 [arXiv:0902.1708 [hep-ph]].
- ¹⁴¹⁸ [55] H. Ishino *et al.* [Belle Collaboration], Phys. Rev. Lett. **98** (2007) 211801 [arXiv:hep-ex/0608035].
- ¹⁴¹⁹ [56] J. P. Lees et al. [BaBar Collaboration], Phys. Rev. D 87 (2012) 052009 [arXiv:1206.3525 [hep-ph]].
- ¹⁴²⁰ [57] J. Beringer et al. [Particle Data Group Collaboration], Phys. Rev. D 86, 010001 (2012).
- [58] Y. Amhis *et al.* [Heavy Flavor Averaging Group], [arXiv:1207.1158 [hep-ex]], and updates at http:
 //www.slac.stanford.edu/xorg/hfag/.
- ¹⁴²³ [59] M. Gronau, Phys. Lett. B **627** (2005) 82 [arXiv:hep-ph/0508047].
- ¹⁴²⁴ [60] M. Fujikawa et al. [Belle Collaboration], Phys. Rev. D 81 (2010) 011101 [arXiv:0809.4366 [hep-ex]].
- ¹⁴²⁵ [61] J. Charles *et al.* [CKM Fitter Group], Phys. Rev. D **84** (2011) 033005 [arXiv:1106.4041 [hep-ph]].
- ¹⁴²⁶ [62] B. Aubert *et al.* [BaBar Collaboration], Phys. Rev. D **81** (2010) 051101 [arXiv:0912.2453 [hep-ex]].
- ¹⁴²⁷ [63] K. Hara *et al.* [Belle Collaboration], Phys. Rev. D 82 (2010) 071101 [arXiv:1006.4201 [hep-ex]].

- ¹⁴²⁸ [64] J. P. Lees *et al.* [BaBar Collaboration], [arXiv:1207.0698 [hep-ex]].
- ¹⁴²⁹ [65] I. Adachi et al. [Belle Collaboration], Phys. Rev. Lett. **110** (2013) 131801 [arXiv:1208.4678 [hep-ex]].
- [66] CDF B-physics results may be found at http://www-cdf.fnal.gov/physics/new/bottom/bottom.
 html.
- ¹⁴³² [67] DO B-physics results may be found at http://www-d0.fnal.gov/Run2Physics/WWW/results/b.htm.
- ¹⁴³³ [68] A. A. Alves, Jr. *et al.* [LHCb Collaboration], JINST **3**, S08005 (2008).
- ¹⁴³⁴ [69] R. Aaij *et al.*, JINST 8, P04022 (2013) [arXiv:1211.3055 [hep-ex]].
- [70] R. Aaij *et al.* [LHCb Collaboration], LHCb-PUB-2012-006, Eur. Phys. J. C 73, 2373 (2013)
 [arXiv:1208.3355 [hep-ex]]; See also a summary in LHCb-PUB-2012-009.
- ¹⁴³⁷ [71] I. Bediaga *et al.* [LHCb Collaboration] CERN-LHCC-2012-007 ; LHCb-TDR-12.
- ¹⁴³⁸ [72] S. Stone and L. Zhang, Phys. Rev. D **79**, 074024 (2009) [arXiv:0812.2832 [hep-ph]].
- ¹⁴³⁹ [73] R. Aaij et al. [LHCb Collaboration], Phys. Rev. D 86, 052006 (2012) [arXiv:1204.5643 [hep-ex]].
- ¹⁴⁴⁰ [74] S. Chatrchyan *et al.* [CMS Collaboration], JHEP **1204**, 033 (2012) [arXiv:1203.3976 [hep-ex]].
- ¹⁴⁴¹ [75] G. Aad *et al.* [ATLAS Collaboration], Phys. Lett. B **713**, 387 (2012) [arXiv:1204.0735 [hep-ex]].
- ¹⁴⁴² [76] D. M. Straub, arXiv:1205.6094 [hep-ph].
- ¹⁴⁴³ [77] R. Aaij *et al.* [LHCb Collaboration], arXiv:1304.6325 [hep-ex].
- ¹⁴⁴⁴ [78] [CMS Collaboration], CMS-PAS-BPH-11-009, 2013.
- ¹⁴⁴⁵ [79] [ATLAS Collaboration], ATLAS-CONF-2013-038, 2013.
- ¹⁴⁴⁶ [80] R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. Lett. 110, **241802** (2013) [arXiv:1303.7125 [hep-ex]].
- ¹⁴⁴⁷ [81] R. Aaij et al. [LHCb Collaboration], JHEP **1206**, 058 (2012) [arXiv:1204.1620 [hep-ex]].
- ¹⁴⁴⁸ [82] R. Aaij *et al.* [LHCb Collaboration], JHEP **1206**, 141 (2012) [arXiv:1205.0975 [hep-ex]].
- ¹⁴⁴⁹ [83] R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. D **85**, 091103 (2012) [arXiv:1202.5087 [hep-ex]].
- ¹⁴⁵⁰ [84] R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. Lett. 110, **222001** (2013) [arXiv:1302.6269 [hep-ex]].
- ¹⁴⁵¹ [85] R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. D **85**, 112004 (2012) [arXiv:1201.5600 [hep-ex]].
- ¹⁴⁵² [86] R. Aaij et al. [LHCb Collaboration], Phys. Lett. B **724** (2013) [arXiv:1304.4518 [hep-ex]].
- ¹⁴⁵³ [87] LHCb-CONF-2012-014; V. A. M. Heijne [LHCb Collaboration], Frascati Phys. Ser. 56, 162 (2012).
- [88] D. M. Asner, T. Barnes, J. M. Bian, I. I. Bigi, N. Brambilla, I. R. Boyko, V. Bytev and K. T. Chao et al., Int. J. Mod. Phys. A 24, S1 (2009) [arXiv:0809.1869 [hep-ex]].
- ¹⁴⁵⁶ [89] M. Gersabeck [LHCb Collaboration], arXiv:1209.5878 [hep-ex].
- ¹⁴⁵⁷ [90] B. I. Eisenstein *et al.* [CLEO Collaboration], Phys. Rev. D 78, 052003 (2008) [arXiv:0806.2112 [hep-ex]].
- ¹⁴⁵⁸ [91] G. Rong, arXiv:1209.0085 [hep-ex].
- ¹⁴⁵⁹ [92] A. Zupanc [Belle Collaboration], arXiv:1212.3942 [hep-ex].
- ¹⁴⁶⁰ [93] A. S. Kronfeld, arXiv:0912.0543 [hep-ph].
- ¹⁴⁶¹ [94] RAaij et al. [LHCb Collaboration], Phys. Rev. Lett. **110**, 101802 (2013) [arXiv:1211.1230 [hep-ex]].
- ¹⁴⁶² [95] A. F. Falk, Y. Grossman, Z. Ligeti and A. A. Petrov, Phys. Rev. D 65, 054034 (2002) [hep-ph/0110317];
- A. F. Falk, Y. Grossman, Z. Ligeti, Y. Nir and A. A. Petrov, Phys. Rev. D 69, 114021 (2004) [hep-ph/0402204].
- [96] E. Golowich, J. Hewett, S. Pakvasa and A. A. Petrov, Phys. Rev. D 76, 095009 (2007). [arXiv:0705.3650
 [hep-ph]].

- [97] O. Gedalia, Y. Grossman, Y. Nir and G. Perez, Phys. Rev. D 80, 055024 (2009) [arXiv:0906.1879
 [hep-ph]]. M. Ciuchini et al., Phys. Lett. B 655, 162 (2007). [arXiv:hep-ph/0703204].
- [98] M. Artuso, B. Meadows and A. A. Petrov, Ann. Rev. Nucl. Part. Sci. 58, 249 (2008); A. Ryd and
 A. A. Petrov, Rev. Mod. Phys. 84, 65 (2012); S. Bianco, F. L. Fabbri, D. Benson and I. Bigi, Riv.
 Nuovo Cim. 26N7, 1 (2003); [arXiv:hep-ex/0309021]. G. Burdman and I. Shipsey, Ann. Rev. Nucl.
 Part. Sci. 53, 431 (2003); X. Q. Li, X. Liu and Z. T. Wei, Front. Phys. China 4, 49 (2009).
- ¹⁴⁷³ [99] I. I. Bigi, arXiv:0902.3048 [hep-ph].
- [100] R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. Lett. **108**, 111602 (2012); T. Aaltonen *et al.* [CDF
 Collaboration], Phys. Rev. Lett. **109**, 111801 (2012); New measurements do not confirm those results:
 R. Aaij *et al.* [LHCb Collaboration], Phys. Lett. B **723**, 33 (2013);
- [101] M. Golden and B. Grinstein, Phys. Lett. B 222, 501 (1989); J. Brod, A. L. Kagan and J. Zupan, 1477 Phys. Rev. D 86, 014023 (2012); B. Bhattacharya, M. Gronau and J. L. Rosner, Phys. Rev. D 85, 1478 054014 (2012); I. I. Bigi and A. Paul, JHEP 1203, 021 (2012); G. Isidori, J. F. Kamenik, Z. Ligeti 1479 and G. Perez, Phys. Lett. B 711, 46 (2012); J. Brod, Y. Grossman, A. L. Kagan and J. Zupan, 1480 JHEP 1210, 161 (2012); W. Altmannshofer, R. Primulando, C. -T. Yu and F. Yu, JHEP 1204, 049 1481 (2012); Y. Grossman, A. L. Kagan and J. Zupan, Phys. Rev. D 85, 114036 (2012); H. -Y. Cheng 1482 and C. -W. Chiang, Phys. Rev. D 85, 034036 (2012) [Erratum-ibid. D 85, 079903 (2012)]; G. Hiller, 1483 Y. Hochberg and Y. Nir, Phys. Rev. D 85, 116008 (2012); T. Feldmann, S. Nandi and A. Soni, JHEP 1484 1206, 007 (2012). 1485
- ¹⁴⁸⁶ [102] E. Golowich, J. Hewett, S. Pakvasa and A. A. Petrov, Phys. Rev. D **79**, 114030 (2009).
- ¹⁴⁸⁷ [103] D. Atwood and A. Soni, Phys. Rev. D **68**, 033003 (2003) [hep-ph/0304085].
- [104] N. Brambilla, S. Eidelman, B. K. Heltsley, R. Vogt, G. T. Bodwin, E. Eichten, A. D. Frawley and
 A. B. Meyer *et al.*, Eur. Phys. J. C **71**, 1534 (2011) [arXiv:1010.5827 [hep-ph]].
- ¹⁴⁹⁰ [105] M. Ablikim *et al.* [BESIII Collaboration], arXiv:1303.5949 [hep-ex].
- ¹⁴⁹¹ [106] G. Pakhlova *et al.* [Belle Collaboration], Phys. Rev. Lett. **101**, 172001 (2008) [arXiv:0807.4458 [hep-¹⁴⁹² ex]].
- ¹⁴⁹³ [107] T. Blum *et al.* [USQCD Collaboration], *Lattice QCD at the Intensity Frontier*, http://www.usqcd. ¹⁴⁹⁴ org/documents/13flavor.pdf (2013).
- [108] R. Brower et al. [USQCD Collaboration], Fundamental parameters from future lattice calculations,
 http://www.usqcd.org/documents/fundamental.pdf (2007).
- ¹⁴⁹⁷ [109] J. Laiho, E. Lunghi and R. S. Van de Water, Phys. Rev. D **81**, 034503 (2010) [arXiv:0910.2928 [hep-¹⁴⁹⁸ ph]].
- ¹⁴⁹⁹ [110] G. Colangelo *et al.* [FLAG], Eur. Phys. J. C **71**, 1695 (2011) [arXiv:1011.4408 [hep-lat]].
- ¹⁵⁰⁰ [111] T. Blum *et al.* [RBC and UKQCD Collaborations], Phys. Rev. Lett. **108**, 141601 (2012) ¹⁵⁰¹ [arXiv:1111.1699 [hep-lat]].
- [112] T. Blum et al. [RBC and UKQCD Collaborations], Phys. Rev. D 86, 074513 (2012) [arXiv:1206.5142
 [hep-lat]].
- ¹⁵⁰⁴ [113] P. A. Boyle *et al.* [RBC and UKQCD Collaborations], arXiv:1212.1474 [hep-lat].
- [114] N. H. Christ *et al.* [RBC and UKQCD Collaborations], Phys. Rev. Lett. **105**, 241601 (2010)
 [arXiv:1002.2999 [hep-lat]].
- ¹⁵⁰⁷ [115] P. Junnarkar and A. Walker-Loud, arXiv:1301.1114 [hep-lat].
- [116] N. H. Christ, T. Izubuchi, C. T. Sachrajda, A. Soni and J. Yu [RBC and UKQCD Collaborations],
 arXiv:1212.5931 [hep-lat].

- ¹⁵¹⁰ [117] L. Lellouch and M. Luscher, Commun. Math. Phys. **219**, 31 (2001) [hep-lat/0003023].
- [118] T. Blum *et al.* [RBC and UKQCD Collaborations], Phys. Rev. D 84, 114503 (2011) [arXiv:1106.2714
 [hep-lat]].
- ¹⁵¹³ [119] C. Kelly [RBC and UKQCD Collaborations], PoS LATTICE **2012**, 130 (2012).
- ¹⁵¹⁴ [120] J. Brod and M. Gorbahn, Phys. Rev. D 82, 094026 (2010) [arXiv:1007.0684 [hep-ph]].
- [121] V. Cirigliano, G. Ecker, H. Neufeld, A. Pich and J. Portoles, Rev. Mod. Phys. 84, 399 (2012)
 [arXiv:1107.6001 [hep-ph]].
- ¹⁵¹⁷ [122] M. T. Hansen and S. R. Sharpe, Phys. Rev. D 86, 016007 (2012) [arXiv:1204.0826 [hep-lat]].
- [123] S. -W. Qiu *et al.* [Fermilab Lattice and MILC Collaborations], PoS LATTICE 2011 (2011) 289
 [arXiv:1111.0677 [hep-lat]].
- ¹⁵²⁰ [124] J. P. Lees *et al.* [BaBar Collaboration], Phys. Rev. Lett. **109**, 101802 (2012) [arXiv:1205.5442 [hep-ex]].
- ¹⁵²¹ [125] J. A. Bailey *et al.* [Fermilab Lattice and MILC Collaborations], Phys. Rev. Lett. **109**, 071802 (2012) ¹⁵²² [arXiv:1206.4992 [hep-ph]].
- [126] C. McNeile, C. T. H. Davies, E. Follana, K. Hornbostel and G. P. Lepage [HPQCD Collaboration],
 Phys. Rev. D 85, 031503 (2012) [arXiv:1110.4510 [hep-lat]].
- ¹⁵²⁵ [127] R. Zhou, arXiv:1301.0666 [hep-lat].
- ¹⁵²⁶ [128] W. Detmold, C. -J. D. Lin, S. Meinel and M. Wingate, Phys. Rev. D 87, 074502 (2013) [arXiv:1212.4827 ¹⁵²⁷ [hep-lat]].
- 1528 [129] I. Baum, V. Lubicz, G. Martinelli, L. Orifici and S. Simula, Phys. Rev. D 84, 074503 (2011)
- 1529 [arXiv:1108.1021 [hep-lat]].