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## **Lecture 11    Ch22.1-22-4 Gauss law    iq09**

1. From Coulomb field of point charge to Gauss law.
2. Field due to charges with spherical symmetry.  
Clicker **11.2**: Point charge + a thick spherical conduction shell.
3. Field from charges with cylindrical symmetry. Clicker **10-2**.
4. Clicker **11-1**, A spherical shell + a long rod
5. Field due to charges with planar symmetry: Clicker **9-2**
  - a. One plate field pattern
  - b. Capacitor plate field pattern: Superposition principle
  - c. Metal Foil in a capacitor clicker **10-3**.

## **Class Announcements:**

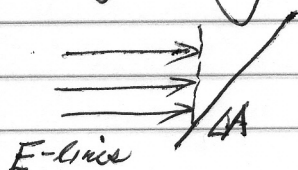
Please go through the physics content of **summary-unit 1** page line by line.

Undergrad assistant, "Summer-CA for Chiu"

- We are looking for an undergrad computer assistant who can convert present handwritten classnotes (posted under the link Lectures in our homepage: <http://www.ph.utexas.edu/~itiq/303Lsp13/chiu/> ) into quality editable efiles.
  - The text will be typed in Latex format.
  - The figures will be redrawn using an appropriate free download illustrator application so that each figure is editable.
- The applicant need to submit following documents together with his/her CV application to Lisa Gentry, [ugaffairs@physics.utexas.edu](mailto:ugaffairs@physics.utexas.edu) The deadline for the application is on Friday, Feb. 15.

# 1. From Coulomb's field of a point charge to G-law.

We first define electric flux.

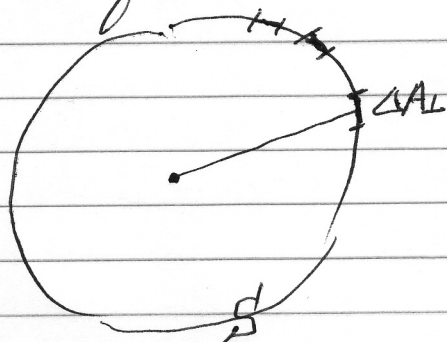


Consider E-line hitting an area  $\Delta A$ .

The electric flux through  $\Delta A$  is defined by

$$\Delta \phi = E \Delta A_{\perp}$$

For point charge  $Q$ , the total electric flux hitting the spherical surface with radius  $r$  is given by



$$\sum_{\text{sphere}} \Delta \phi = \sum_{\text{sphere}} E \Delta A_{\perp}$$

$$= E \sum_{\text{sph}} \Delta A_{\perp} = E 4\pi r^2$$

$$= \frac{kQ}{r^2} \cdot 4\pi r^2 = 4\pi kQ = \frac{Q}{\epsilon_0}$$

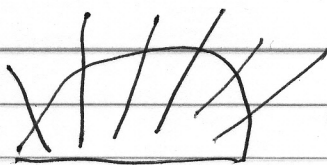
In other words:

$$\text{Total flux emitted by the point charge} = \frac{Q}{\epsilon_0}$$

General statement of Gauss Law. Define Gaussian surface  $S$  to be <sup>the</sup> ~~any~~ surface which enclosed the charge then

flux emitted thru  $S$  equals  $\frac{Q}{\epsilon_0}$ . Thus  $S$  can be

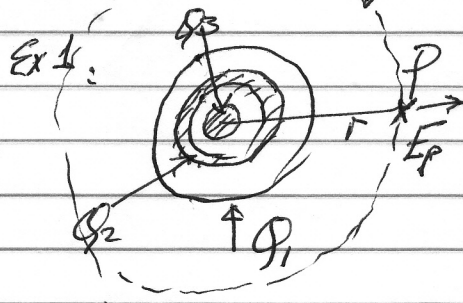
of arbitrary shape,  $Q$  can be any charge distribution within  $S$ .  
We have  $\Phi_S = \frac{Q_S}{\epsilon_0}$ . Pencil-needle analogy:



By counting the middle one can determine the size of the preupine.

GL: Two ingredients:  $\Phi + S$ .

2. Field due to charges which have a spherical symmetry.



Find  $E_p$ .

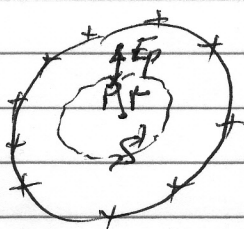
$$\Phi_S = \oint E_p dA_{\perp} = E_p 4\pi r^2 = \frac{Q_1 + Q_2}{\epsilon_0}$$

$$\therefore E_p = \frac{(Q_1 + Q_2 + Q_3)}{4\pi\epsilon_0 r^2}$$

So long as it is spherically symmetric  $E_p = \frac{K(Q_1 + Q_2 + Q_3)}{r^2}$ .

$r < R$ :

Ex 2



$E_p = 0$ . Proof: -

Through P, draw Gaussian surface S.

$$E_p 4\pi r^2 = \frac{Q_S}{\epsilon_0} = 0 \Rightarrow E_p = 0.$$

Clicker 11-2

Given:  $Q$  at 0. Surface charges on the thin metal shell. Inner surface:  $Q'$ , outer surface  $Q''$ . (Proof there is no charge in the interior of the conducting shell, charges can only reside on the surface)

11-22.  $\Phi_S = ?$   $\oint E dA_{\perp} = ?$  Why must it be 0

11-2b. Determine  $Q'$  and  $Q''$ . Assume no charge on conducting shell is  $Q$ ,

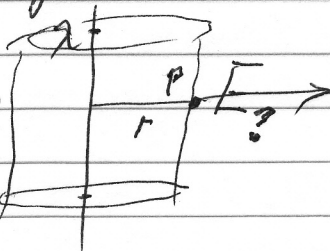
Gauss Law:  $\Phi_E = 0 = \frac{Q + Q'}{\epsilon_0} \therefore Q' = -Q$

What's  $Q''$ ? Ans:  $Q + Q'' = Q$ ,  $Q'' = Q - Q' = Q$   
 $\therefore$  Ans = choice 1.

Q with Cylindrical Symmetry:

Given: Long uniformly charged rod

$$\lambda = \frac{\Delta Q}{\Delta y}$$



Find: Field at P.

Gaussian surface - Cylinder through P

$E$ ? Radially out ward

$$\Phi_E = \oint E \cdot dA = \frac{Q_{\text{enc}}}{\epsilon_0}$$

$$E \oint dA = L 2\pi r E = \frac{\lambda L}{\epsilon_0}$$

$$\therefore E = \frac{\lambda}{2\pi \epsilon_0 r} \quad \text{Ans = 2}$$

Agree with integration result for  $\frac{L}{2} \gg R$ .

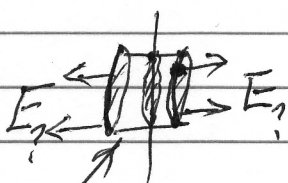
$$E_x = \frac{k\lambda L}{x^2} \int_{-\frac{L}{2}}^{+\frac{L}{2}} \frac{1}{r^2} dx = \frac{k\lambda}{x} \cdot \frac{L}{(\frac{L}{2})} = \frac{2k\lambda}{x} = \frac{1}{2\pi\epsilon_0} \cdot \frac{\lambda}{r}$$



3. Planar symmetry case plate:

From analytic ~~and~~ integration results we have

$$E_x = \frac{\sigma}{2\epsilon_0} = \frac{\Delta Q / \Delta A}{2\epsilon_0}$$

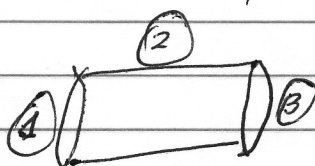


Gaussian Surface S

$$\Phi_S = \frac{Q_S}{\epsilon_0}$$

$\Delta Q$  in the shaded area

$\Delta A$ : Ends of the cylinder



$$\Phi = EA_{\perp} \Rightarrow \Phi_S = \Phi_1 + \Phi_2 + \Phi_3 = 2E_x \Delta A = \frac{\Delta Q}{\epsilon_0}$$

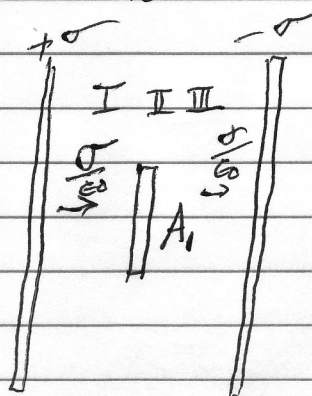
$$E_x \Delta A \quad \quad \quad 0 \quad \quad \quad E_x \Delta A$$

$E_{\perp} \text{ to } \Delta A$

$$\therefore E_x = \frac{\Delta Q / 2\Delta A}{\epsilon_0} = \frac{\sigma}{2\epsilon_0}$$

There is no field which passes thru  $\Delta A$

Checker 10-3



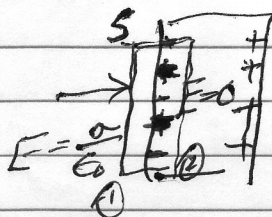
Without foil:  $\frac{\sigma}{\epsilon_0}$  through  $\Delta A$

With foil

$$\Phi_S = \frac{Q_S}{\epsilon_0}$$

$$\textcircled{1} + \textcircled{2}$$

$$\frac{\sigma}{\epsilon_0} A_1 + 0 = \frac{Q_{\text{left}}}{\epsilon_0}$$



$$Q_{\text{left}} = \sigma A_1 \quad \underline{\text{Ans: 1}}$$