
Lecture36 iq32

Maxwell equations and 1D plane EM waves

1. LC and LRC circuits: The amped envelop
2. Maxwell equations:
 - a. Gauss law
 - b. Gauss law for magnetism: No magnetic monopole
 - c. Ampere-Maxwell law
 - i. Piercing through a plane film
 - ii. Piercing through 3D film which includes E-flux in the gap
 - iii. Partial piercing
3. Ch24.h1: 15-16. 1D plane EW aves.
 - a. Switch on the current sheet at $t=0$.
 - b. B-flux passing through the front window 12341 and Faraday's law
 - c. E-flux passing through the top area 12561 and Ampere-Maxwell's law
 - d. $v^2=1/(\epsilon_0 \times \mu_0)$
 - e. Measurement of ϵ_0 and μ_0 in static experiments.

Reflection: Faraday law and Ampere-Maxwell's law enable the propagation of EM waves in vacuum.

Announcement:

Midterm 3, class average 71.

The lecture video in our homepage is now available for viewing. Keep in mind it is an experimental project. Your feedback is welcome.

Application of the LA position is now available. For those of you who do well in this course are encouraged to apply the LA job. LAs are playing an important part in helping students through their interaction with students. If you are interested in this job opportunity please contact Lisa Gentry*.

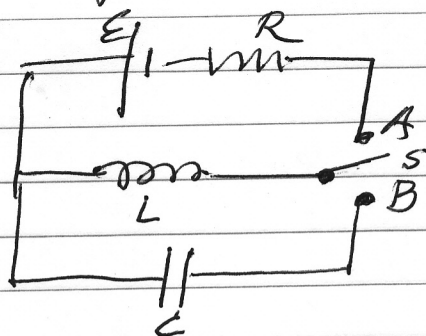
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RLC circuit

Typical set up to get LC oscillation started



S at A to build up current.

S from A to B begin osc. max I in L

Lenz Rule controls current flow charging the plate.

Typical oscillator cycle: Fig 32.01a
 $t=0 \rightarrow t=T/2$

Neutralize plate charge: CCW current

from $t=T/2 \rightarrow T$: CW current

Loop eqn: $\mathcal{E} - L \frac{dI}{dt} - \frac{q}{C} - IR = 0$

Potential eqn: $I\mathcal{E} - \frac{d}{dt} \left(\frac{LI^2}{2} + \frac{q^2}{2C} \right) - IR^2 = 0$

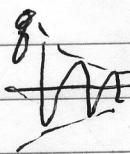
$U_{\text{max}} = U_{\text{Lmax}} = U_L + U_C$

$\mathcal{E}=0, R=0$, conservation of energy $\frac{d}{dt}(U_L + U_C) = P_L + P_C = 0$

$\mathcal{E}=0, R \neq 0$

$\underbrace{P_L + P_C}_{\text{negative}} + I^2 R = 0$

Damped envelope



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Maxwell eqn -

- Gauss Law

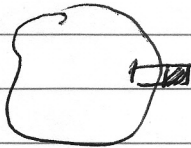
$$\oint \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$$

- Magnetic Gauss Law

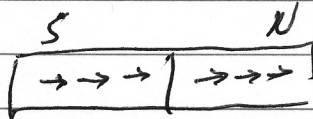
$$\oint \mathbf{B} \cdot d\mathbf{A} = 0 \quad (\text{no magnetic charge})$$

magnetic charge enters in the form of dipole

Can we have?



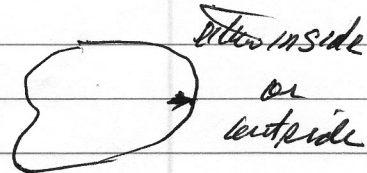
At microscopic level



Dipole orbital current loop

spin: μ_B

Dipole present as fundamental unit



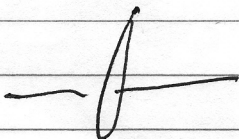
- Ampere's Law -

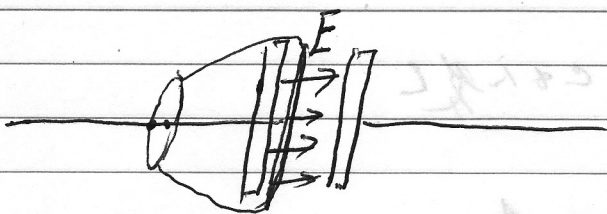
$$\oint_{\text{path}} \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_{\text{enc}}$$

Current piercing the surface where the

rim of the surface = path

straight wire





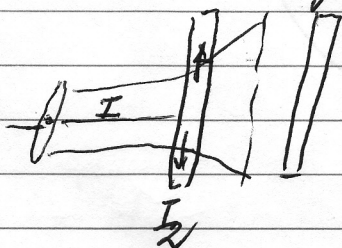
$$E = \frac{Q/A}{\epsilon_0}, \quad Q = \epsilon_0 EA$$

Q on the plate, it quantifies E -flux

responsible for piercing the surface defined by the rim

$$\frac{dQ}{dt} = \epsilon_0 \frac{d\Phi_E}{dt} \quad (\text{virtual current, displacement current})$$

Partial piercing:



$$RHS = \epsilon_0 \left[I + \epsilon_0 \frac{d\Phi}{dt} \right]$$

partial piercing

$$I_2 + \epsilon_0 \frac{d\Phi_2}{dt}$$

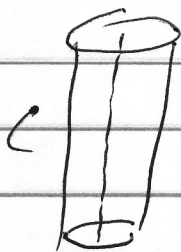
Difficult to understand.

How can em waves propagate in vacuum?

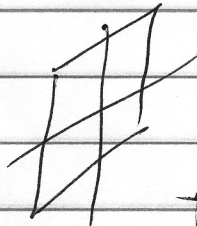
Why should it work in the same way as mechanical waves require the presence of a medium?

How 1D plane waves propagate?

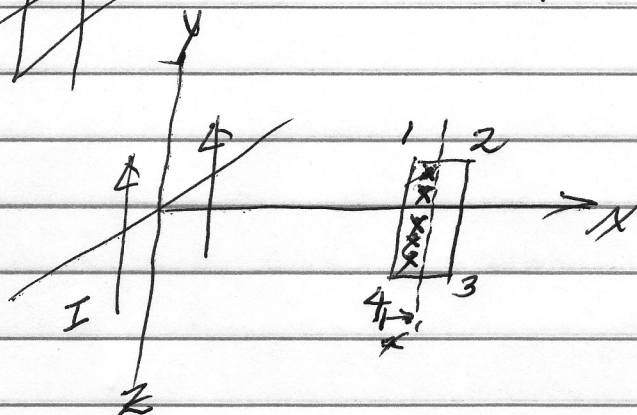
Drop a pebble in a pond $\rightarrow$ See circular wavefront (adjacent pts with same phase)



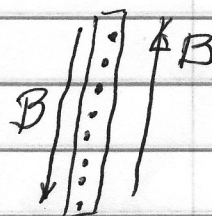
Cylindrical wavefront



Sheet of current $\Rightarrow$ 1d waves
plane waves.



Top view:



HW Ch24.41

$$Eh = \frac{Bh v}{\frac{dBx}{dt}}$$

"B_{in}"

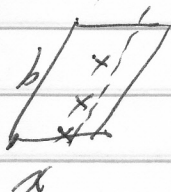
E_{in}



$$E = Bv$$

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A-M: path



$$\oint B \cdot dl = \mu_0 \left[\epsilon_0 \frac{d\Phi_E}{dt} \right]$$

$$\frac{d(Ebx)}{dt} = Ebv$$

$$Bb = \mu_0 \epsilon_0 Ebv$$

$$B = \mu_0 \epsilon_0 v^2 E, \quad v = \frac{1}{\sqrt{\mu_0 \epsilon_0}} \approx 3 \times 10^8 \text{ m/s}$$

$$\frac{1}{\mu_0 \epsilon_0} = \frac{4\pi}{\mu_0} \cdot \frac{1}{4\pi \epsilon_0} = 107 \times 9 \times 10^9 = (3 \times 10^8)^2$$

all em waves in vac $\approx 3 \times 10^8 \text{ m/s}$

Measure μ_0 :

$$F_{I_2 I_1} = \left(\frac{\mu_0 I_1}{2\pi r} \right) \left(\frac{\mu_0 I_2}{2\pi r} \right) \uparrow \uparrow$$

$$\text{Measure } \epsilon_0: F = \frac{qQ}{4\pi \epsilon_0 r^2}$$