- 1. First, solve problem  $\mathbf{1}(d)$  of the previous homework set.
- Second, an easy reading assignment: The 4-page note I distributed in class (also available on-line at the homework page). Make sure you understand all the algebra: You may need to perform a similar calculation in the future.
- 3. And now, a calculational exercise: Verify that at the one-loop level  $\delta_1 = \delta_2$ , including the finite parts of both counterterms.
  - (a) Continue the classroom calculation of one-loop vertex correction for the special case of q = 0. Derive an exact formula for the  $F_1^{1 \text{ loop}}(q^2 = 0)$  and hence for the  $\delta_1$  counterterm in D dimensions. Do not take the  $D \to 4$  limit.

To regularize the IR divergence, assume the photon to have a tiny but non-zero mass  $m_{\gamma} \ll M_e$ , hence photon propagator

$$\frac{-ig^{\mu\nu}}{k^2 - m_{\gamma}^2 + i0} \,. \tag{1}$$

(b) And now calculate the  $\Sigma^{1 \text{ loop}}(p)$  for the electron in D dimensions, without taking the  $D \to 4$  limit. Then evaluate the derivative  $d\Sigma^{1 \text{ loop}}/dp$  for  $p = M_e$  and hence the  $\delta_2$  counterterm.

Note that for  $\not p = m$ , the derivative develops an infrared divergence. To regularize this divergence, use a tiny photon mass, exactly as in part (a).

- (c) Verify that  $\delta_1 = \delta_2$  in any dimension *D*. If you do not achieve this equality, check your calculations for mistakes.
- 4. And finally, another reading assignment: §6.1 of the *Peskin & Schroeder* textbook. The soft-photon bremsstrahlung discussed there is important for understanding the infra-red divergences of QED.