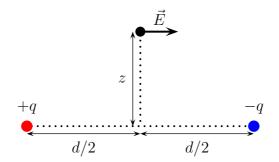
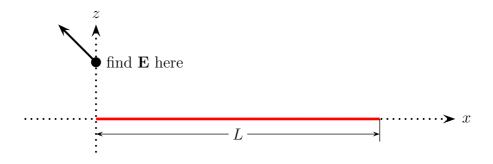
**Problem 2.2:** Find the electric field **E** (both the magnitude and the direction) at distance z above the midpoint between two equal and opposite point charges  $\pm q$ , at distance d apart from each other.

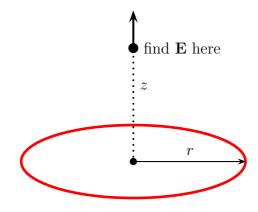


**Problem 2.3:** Find the electric field **E** directly above one end of a straight line segment of length L that carries a uniform line charge  $\lambda$ .

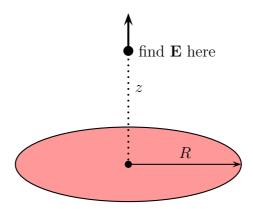


Check that your formula is consistent with what you would expect for  $z \gg L$ .

**Problem 2.5:** Find the electric field at height z directly above the center of a circular loop of radius r carrying uniform line  $\lambda$ .



**Problem 2.6:** Find the electric field at height z directly above the center of a flat circular disk of radius R that carries a uniform surface charge  $\sigma$ .



What does your formula give in the limit of  $R \to \infty$ ? Also, check the opposite limit of  $z \gg R$ .

Problem 1.6: Prove that

 $\mathbf{A} \times (\mathbf{B} \times \mathbf{C}) + \mathbf{B} \times (\mathbf{C} \times \mathbf{A}) + \mathbf{C} \times (\mathbf{A} \times \mathbf{B}) = \mathbf{0}.$ 

Also, under what conditions  $\mathbf{A} \times (\mathbf{B} \times \mathbf{C}) = (\mathbf{A} \times \mathbf{B}) \times \mathbf{C}$ ?

**Problem 1.11:** Find the gradients of the following functions:

(a) 
$$f(x, y, z) = x^2 + y^3 + z^4$$
.  
(b)  $f(x, y, z) = x^2 y^3 z^4$ .  
(c)  $f(x, y, z) = e^x \sin(y) \ln(z)$ .

**Problem 1.13:** Let  $\vec{\mathcal{R}} = \mathbf{r} - \mathbf{R}_0$  be the radius vector from a fixed point  $\mathbf{R}_0 = (X_0, Y_0, Z_0)$  to the point  $\mathbf{r} = (x, y, z)$  we follow, and let  $\mathcal{R} = |\vec{\mathcal{R}}|$  be its length, *i.e.* the distance between the points  $\mathbf{R}_0$  and  $\mathbf{r}$ . Consider the gradients of powers of this distance  $\mathcal{R}$  with respect to  $\mathbf{r}$  (while the  $\mathbf{R}_0$  is held fixed). Show that

(a) 
$$\nabla(\mathcal{R}^2) = 2\vec{\mathcal{R}};$$
  
(b)  $\nabla(1/\mathcal{R}) = -\vec{\mathcal{R}}/\mathcal{R}^3;$   
(c) what is the general formula for the  $\nabla(\mathcal{R}^n)$ ?

## Postponed to homework set#2

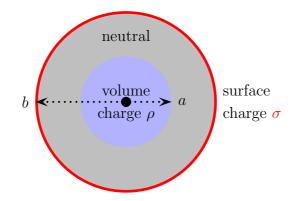
**Problem 2.15:** A thick spherical shell of inner radius a and outer radius b carries a nonuniform (but spherically symmetric) charge density

$$\rho(r) = \frac{k}{r^2} \quad \text{[for } a \le r \le b \text{ only]}.$$

Find the electric field in the three regions: (i) r < a, (ii) a < r < b, (iii) r > b. Plot  $|\mathbf{E}|$  as a function of the radius r for the case of b = 2a.

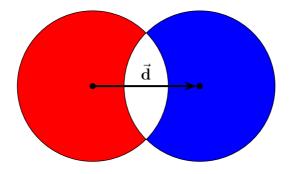
**Problem 2.16:** Conside a *long* coaxial cable comprised of the inner cylinder of radius a and the outer cylindric shell from a to b. The inner cylinder carries a uniform *volume* charge density  $\rho$ . The outer shell has no volume charges but on its outer surface (at r = b) it has a uniform *surface* charge density  $\sigma$ . The sign of  $\sigma$  is opposite to  $\rho$  and its magnitude is such

that the whole cable has zero net charge. Here is what the cable's cross-section looks like:



Find the electric field in each of the three regions: (i) r < a, inside the inner cylinder; (ii) a < r < b, inside the outer shell; (iii) r > b, outside the cable. Plot  $|\mathbf{E}|$  as a function of the radius r.

**Problem 2.18:** Two spheres of the same radius R and containing equal and opposite volume charge densities — respectively,  $+\rho$  and  $-\rho$  — are placed so that they partially overlap. The overlapping region is rendered neutral.



Show that the electric field in the overlapping region is uniform and calculate its value as a function of the vector  $\mathbf{d}$  from the positive center to the negative center.

Hint: first, use the Gauss Law to calculate the electric field inside a uniformly charged solid sphere, *cf.* problem 2.12.