Problem 2.2: Find the electric field $\mathbf{E}$ (both the magnitude and the direction) at distance $z$ above the midpoint between two equal and opposite point charges $\pm q$, at distance $d$ apart from each other.


Problem 2.3: Find the electric field $\mathbf{E}$ directly above one end of a straight line segment of length $L$ that carries a uniform line charge $\lambda$.


Check that your formula is consistent with what you would expect for $z \gg L$.

Problem 2.5: Find the electric field at height $z$ directly above the center of a circular loop of radius $r$ carrying uniform line $\lambda$.


Problem 2.6: Find the electric field at height $z$ directly above the center of a flat circular disk of radius $R$ that carries a uniform surface charge $\sigma$.


What does your formula give in the limit of $R \rightarrow \infty$ ? Also, check the opposite limit of $z \gg R$.

Problem 1.6: Prove that

$$
\mathbf{A} \times(\mathbf{B} \times \mathbf{C})+\mathbf{B} \times(\mathbf{C} \times \mathbf{A})+\mathbf{C} \times(\mathbf{A} \times \mathbf{B})=\mathbf{0}
$$

Also, under what conditions $\mathbf{A} \times(\mathbf{B} \times \mathbf{C})=(\mathbf{A} \times \mathbf{B}) \times \mathbf{C}$ ?

Problem 1.11: Find the gradients of the following functions:

$$
\begin{aligned}
& \text { (a) } f(x, y, z)=x^{2}+y^{3}+z^{4} \\
& \text { (b) } f(x, y, z)=x^{2} y^{3} z^{4} . \\
& \text { (c) } f(x, y, z)=e^{x} \sin (y) \ln (z) .
\end{aligned}
$$

Problem 1.13: Let $\overrightarrow{\mathcal{R}}=\mathbf{r}-\mathbf{R}_{0}$ be the radius vector from a fixed point $\mathbf{R}_{0}=\left(X_{0}, Y_{0}, Z_{0}\right)$ to the point $\mathbf{r}=(x, y, z)$ we follow, and let $\mathcal{R}=|\overrightarrow{\mathcal{R}}|$ be its length, i.e. the distance between the points $\mathbf{R}_{0}$ and $\mathbf{r}$. Consider the gradients of powers of this distance $\mathcal{R}$ with respect to $\mathbf{r}$ (while the $\mathbf{R}_{0}$ is held fixed). Show that
(a) $\nabla\left(\mathcal{R}^{2}\right)=2 \overrightarrow{\mathcal{R}} ;$
(b) $\nabla(1 / \mathcal{R})=-\overrightarrow{\mathcal{R}} / \mathcal{R}^{3}$;
(c) what is the general formula for the $\nabla\left(\mathcal{R}^{n}\right)$ ?

## Postponed to homework set\#2

Problem 2.15: A thick spherical shell of inner radius $a$ and outer radius $b$ carries a nonuniform (but spherically symmetric) charge density

$$
\rho(r)=\frac{k}{r^{2}} \quad[\text { for } a \leq r \leq b \text { only }] .
$$

Find the electric field in the three regions: (i) $r<a$, (ii) $a<r<b$, (iii) $r>b$. Plot $|\mathbf{E}|$ as a function of the radius $r$ for the case of $b=2 a$.

Problem 2.16: Conside a long coaxial cable comprised of the inner cylinder of radius $a$ and the outer cylindric shell from $a$ to $b$. The inner cylinder carries a uniform volume charge density $\rho$. The outer shell has no volume charges but on its outer surface (at $r=b$ ) it has a uniform surface charge density $\sigma$. The sign of $\sigma$ is opposite to $\rho$ and its magnitude is such
that the whole cable has zero net charge. Here is what the cable's cross-section looks like:


Find the electric field in each of the three regions: (i) $r<a$, inside the inner cylinder; (ii) $a<r<b$, inside the outer shell; (iii) $r>b$, outside the cable. Plot $|\mathbf{E}|$ as a function of the radius $r$.

Problem 2.18: Two spheres of the same radius $R$ and containing equal and opposite volume charge densities - respectively, $+\rho$ and $-\rho$ - are placed so that they partially overlap. The overlapping region is rendered neutral.


Show that the electric field in the overlapping region is uniform and calculate its value as a function of the vector $\mathbf{d}$ from the positive center to the negative center.

Hint: first, use the Gauss Law to calculate the electric field inside a uniformly charged solid sphere, $c f$. problem 2.12.

